# Measurement of elliptic and higher-order flow harmonics at $2.76 \mathrm{TeV} \mathrm{Pb+Pb}$ collisions with the ATLAS detector. 



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## Azimuthal anisotropy in heavy ion collisions



Pressure gradients lead to azimuthal anisotropy


Fourier harmonics $v_{n}=\left\langle\cos \left(n\left(\Phi-\Psi_{n}\right)\right)\right\rangle$

- Initial shape of the interaction region ( $\mathrm{v}_{2}$ - elliptic flow)
- Initial spatial fluctuations of interacting nucleons (higher orders, $\mathbf{v}_{\mathrm{n}}$ )


## ATLAS detector



Centrality determination


- Energy deposited in entire FCal ( $3.1<|n|<4.9$ ) is used for centrality determination
- Event plane measurement is based on energy deposition in the first sampling layer of FCal
 is a composite tracking system consisting of silicon and gaseous detectors.

Three tracking techniques:

- ID tracks:
$p_{T}>0.5 \mathrm{GeV}$
- Pixel tracks:
$p_{T}>0.1 \mathrm{GeV}$
- Two point pixel tracklets (B-off): $\mathrm{p}_{\mathrm{T}}>0.03 \mathrm{GeV}$



## Integrated $\mathrm{v}_{2}$ down to very low $\mathrm{p}_{\mathrm{T}}$

- Integrated $\mathrm{v}_{2}$ flow harmonic measured using the EP method
- Reaching low $p_{T}$ reduces uncertainty on the integrated $\mathrm{v}_{2}$

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ID tracks $p_{T}>0.5 \mathrm{GeV}$

Pixel tracks - varied lower integration $p_{T}$ limit to link ID tracks and tracklets

Tracklets $p_{T}>0.03 \mathrm{GeV}$

## Pseudorapidity dependence of integrated $\mathbf{v}_{2}$

- $\mathrm{v}_{2}(\mathrm{\eta})$ integrated over $\mathrm{p}_{\mathrm{T}}$, shows weak pseudorapidity dependence
- $\mathrm{v}_{\mathbf{2}}(\boldsymbol{\eta})$ scaling with $\boldsymbol{\eta}-\mathrm{y}_{\text {beam }}$ consistent with the trend observed by PHOBOS at RHIC (Phys.Rev.C72:051901,2005)

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## Pseudorapidity dependence of $\mathbf{v}_{2}$



- No substantial $\eta$ dependence for any $p_{T}$ or centrality interval is observed ( $\mathrm{v}_{2}$ drops by about 5-10\% over the range $|\eta|=0-2.4$ )
- Different from PHOBOS measurements at RHIC in which $\mathrm{v}_{2}$ decreases by ~30\% within the same $\eta$ range (PHOBOS Phys. Rev. C72 (2005) 051901)


## Higher order flow harmonics - $p_{T}$ dependence

- The $\mathrm{p}_{\mathrm{T}}$-dependence of $\mathrm{v}_{2}-\mathrm{v}_{6}$ for several centrality selections
- Similar $p_{T}$-dependence for all harmonics
- $\mathrm{v}_{\mathrm{n}}$ generally decreases for larger $n$, except in the most central events:
- $\mathrm{v}_{3}$ dominates in $\mathrm{p}_{\mathrm{T}}$ range ~2-7 GeV
$-\mathrm{v}_{4}>\mathrm{v}_{2}$ in $\mathrm{p}_{\mathrm{T}}$ range $\sim 3-5 \mathrm{GeV}$



## Two-particle correlation method



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The two-particle correlation function: $C(\Delta \phi, \Delta \eta)=\frac{N_{s}(\Delta \phi, \Delta \eta)}{N_{m}(\Delta \phi, \Delta \eta)} \quad \begin{aligned} & \begin{array}{l}\mathbf{N}_{s}-\text { same event pairs } \\ \mathbf{N}_{\mathrm{m}}-\text { mixed event pairs }\end{array}\end{aligned}$

$\mathbf{v}_{\mathrm{n}, \mathrm{n}}$ are calculated via Discrete Fourier


$$
\text { Transform (DFT) : } \quad \sum_{m} \cos \left(n \Delta \phi_{m}\right) C\left(\Delta \phi_{m}\right)
$$

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$\mathrm{N}_{\mathrm{s}}$ - same event pairs
$\mathbf{N}_{\mathrm{m}}$ - mixed event pairs

Projected onto $\Delta \varphi$
1D correlation function

$$
\frac{d N}{d \Delta \phi} \propto 1+2 \sum_{n} v_{n, n} \cos (n \Delta \phi)
$$


$\mathbf{v}_{\mathrm{n}, \mathrm{n}}$ are calculated via Discrete Fourier

$$
\begin{aligned}
& \text { Transform (DFT) : } v_{n, n}=<\cos (n \Delta \phi)>=\frac{\sum_{m} \cos \left(n \Delta \phi_{m}\right) C\left(\Delta \phi_{m}\right)}{\sum_{m} C\left(\Delta \phi_{m}\right)}
\end{aligned}
$$

It is expected that for flow modulations:

$$
v_{n, n}\left(p_{T}^{a}, p_{T}^{b}\right)=v_{n}\left(p_{T}^{a}\right) v_{n}\left(p_{T}^{b}\right)
$$

And for "fixed-pT" correlations:

$$
v_{n}=\sqrt{V_{n, n}}
$$




## Two particle correlation vs EP results

$$
C(\Delta \Phi)=b^{2 \mathrm{PC}}\left(1+2 \mathrm{v}_{1,1}^{2 \mathrm{PC}} \cos \Delta \Phi+2 \sum_{n=2}^{6} v_{n}^{E P, a} v_{n}^{E P, b} \cos n \Delta \Phi\right)
$$

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$\Delta \phi$

- $b^{2 P C}$ average of the correlation function
- $\mathrm{v}_{1,1}{ }^{2 \mathrm{PC}}$ first harmonic from the 2PC analysis
- Other $\mathrm{v}_{\mathrm{n}}$ components measured with the event plane method
- Correlation function reproduced very well
even harmonics contribution
odd harmonics
contribution


## Elliptic flow with cumulant method

- Elliptic flow harmonics of charged particles obtained with the cumulant generating function method
(N. Borghini, P.M.Dinh and J.Y. Ollitrault Phys.Rev.C 64 (2001) 054901)

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- $\mathrm{v}_{2}$ measurement (e.g. with the Event Plane method) is distorted by non-flow effects (not related to initial geometry)
- Cumulants of multi-particle (>2) correlations eliminates non flow contributions



## Comparison of $\mathrm{v}_{2}\{2\}, \mathrm{v}_{2}\{4\}$ and $\mathrm{v}_{2}\{E P\}$

- Strong reduction of $\mathrm{v}_{2}$ is observed by using four-particle cumulants
- $\mathrm{v}_{2}\{4\}$ consistent between ATLAS, ALICE and CMS
- The $\mathrm{v}_{2}\{E P\}$ lies between $\mathrm{v}_{2}\{2\}$ and $\mathrm{v}_{2}\{4\}$

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## Elliptic flow fluctuations (cumulant method)

- Cumulant method provides a measure of elliptic flow event-by-event fluctuations (N. Borghini, P.M.Dinh and J.Y. Ollitrault Phys.Rev. C64 (2001) 054901)


$$
\frac{\sigma_{2}}{<\mathrm{v}_{2}>} \approx \sqrt{\frac{\mathrm{v}_{2}\{2\}^{2}-\mathrm{v}_{2}\{4\}^{2}}{\mathrm{v}_{2}\{2\}^{2}+\mathrm{v}_{2}\{4\}^{2}}}
$$

- For the 5-10\% centrality fluctuations independent of $p_{T}$
W. Broniowski, M. Rybczyński, P. Bożek arXiv:0710.5731
- For less central collisions $\sigma_{2} /\left\langle\mathrm{v}_{2}\right\rangle$ increases with $\mathrm{p}_{\mathrm{T}}$
- $\sigma_{2} /<v_{2}>$ agrees with the Glauber MC model prediction with the except of peripheral collisions
 centrality intervals


## Summary

- ATLAS measured integrated $\mathrm{v}_{2}$ flow harmonic reaching very low $p_{T}$
- Differential $\mathrm{v}_{2}$ and higher order flow harmonics were measured with various methods in wide $p_{T}, \eta$ and centrality range
- $\mathbf{v}_{\mathrm{n}}\left(\mathrm{p}_{\mathrm{T}}\right)$ shows the same trends
- rise up to $\sim 3 \mathrm{GeV}$
- decrease within 3-8 GeV
- varies weakly at high $p_{T}$
- $\mathbf{v}_{\mathrm{n}}(\mathrm{\eta})$ remains approximately constant
- Relative fluctuations of elliptic flow from 2- and 4-particle cumulants are consistent with the Glauber MC model



## $p_{T}$ dependence of the $\mathbf{v}_{2}$ of charged particles

- All centrality intervals shows:
- Rapid rise in $\mathrm{v}_{2}\left(\mathrm{p}_{\mathrm{T}}\right)$ up to $\mathrm{p}_{\mathrm{T}} \sim 3 \mathrm{GeV}$
- Decrease out to 7-8 GeV
- Weak $\mathrm{p}_{\mathrm{T}}$-dependence above 9-10 GeV
- The strongest elliptic flow at LHC is observed in centralities 30-50\%


## Event plane determination

- Reaction plane ( $\Psi$ RP) is approximated by event plane ( $\Psi_{\mathrm{n}}{ }^{\text {EP }}$ ) measured in FCal:

$$
\Psi_{n}^{E P}=\frac{1}{n} \tan ^{-1} \frac{\sum_{i} E_{T, i}^{\text {tower }} w_{i} \sin \left(n \phi_{i}\right)}{\sum_{i} E_{T, i}^{\text {tower }} w_{i} \cos \left(n \phi_{i}\right)}
$$

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- The event plane resolution correction factor $R$ is obtained using two-sub event and various tree-subevent method
- Significant resolution for harmonics $\mathrm{n}=2$ - 6
- Resolution corrected harmonics:

$$
v_{n}=\left\langle\cos \left(n\left(\Phi-\Psi_{n}\right)\right)\right\rangle / R
$$

## Comparison with ALICE and RHIC experiments



- All data sets are quite consistent for both low and high $p_{T}$


## Higher order harmonics scaling

- Hydrodynamics model suggests scaling $\mathrm{v}_{4} \sim \mathrm{v}_{2}{ }^{2}$ (PHENIX PRL 105, 062301 (2010))
- The $\mathrm{p}_{\mathrm{T}}$-dependence of the $v_{n}{ }^{1 / n / v_{2}}{ }^{1 / 2}$ ( $\mathrm{n}=3-6$ ) ratio for several centrality selections
- Weak $p_{T}$-dependence of the ratio except 5\% most central events
- Ratio for $\mathrm{n}=3$ systematically lower than for $n=4,5$



## Two particle correlation vs EP results



Good agreement between both methods in the selected kinematical range ( $p_{T} 1-3 \mathrm{GeV}, 2<|\eta|<5$ )

