



# The measurement of $f_s/f_d$ from hadronic modes in LHCb experiment

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# Outline



1. Introduction
2. Analysis strategy
  - Selection procedure
  - Signal model
  - Background model
3. Fitting results
4. Systematic uncertainty
5. Results



# Introduction



$f_q$  - fragmentation functions, describe the probability that a  $b$  quark will hadronize into a  $B_q$  meson (where  $q = u, d, s$ ) or  $\Lambda_b$  baryon, respectively.

## ▶ Signal

- $B_d \rightarrow D\pi$  (tree + exchange topology)
- $B_d \rightarrow DK$  (tree topology)
- $B_s \rightarrow D_s\pi$  (tree topology)

## ▶ Data:

- $\sim 35 \text{ pb}^{-1}$  of data collected in 2010

## ▶ Goal:

- Measure  $f_s/f_d$  (important for many BR measurements, e.g.  $B_s \rightarrow \mu\mu$ ) at 7 TeV
- First step towards the measurement of the CP violation in the signal modes.



# Introduction 2



$B_{d \rightarrow DK} / B_{s \rightarrow D_s \pi}$

- Same final state (KK $\pi\pi$ )
- Small theoretical uncertainty 7%

$$\frac{f_s}{f_d} = 0.0743 \times \frac{\tau_{B^0}}{\tau_{B_s^0}} \times \left[ \frac{1}{\mathcal{N}_a \mathcal{N}_F} \frac{\epsilon_{DK}}{\epsilon_{D_s \pi}} \frac{N_{D_s \pi}}{N_{DK}} \right]$$

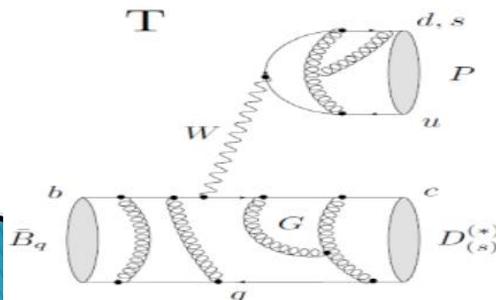
- arXiv:1004.3982v3

Deviation from factorization:

$$\mathcal{N}_a \equiv \left| \frac{a_1(D_s \pi)}{a_1(DK)} \right|^2 = 1.00 \pm 0.02$$

Form factor:

$$\mathcal{N}_F \equiv \left[ \frac{F_0^{(s)}(m_\pi^2)}{F_0^{(d)}(m_K^2)} \right]^2 = 1.24 \pm 0.08$$



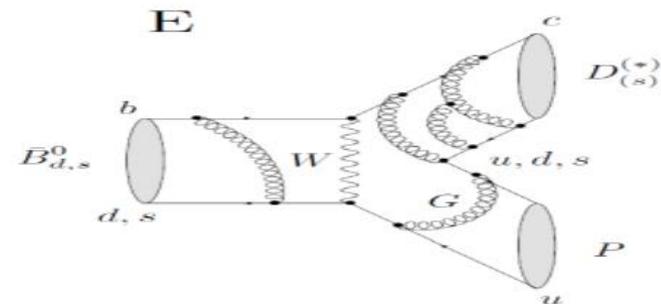
$B_{d \rightarrow D \pi} / B_{s \rightarrow D_s \pi}$

- Similar final states
- Theoretical uncertainty of order of 9%

$$\frac{f_s}{f_d} = 0.982 \times \frac{\tau_{B^0}}{\tau_{B_s^0}} \times \left[ \frac{1}{\tilde{\mathcal{N}}_a \mathcal{N}_F \mathcal{N}_E} \frac{\epsilon_{D \pi}}{\epsilon_{D_s \pi}} \frac{N_{D_s \pi}}{N_{D \pi}} \right]$$

- Additional contribution from the exchange diagrams

$$\mathcal{N}_E = 0.966 \pm 0.056$$



- arXiv:1012.2784v1



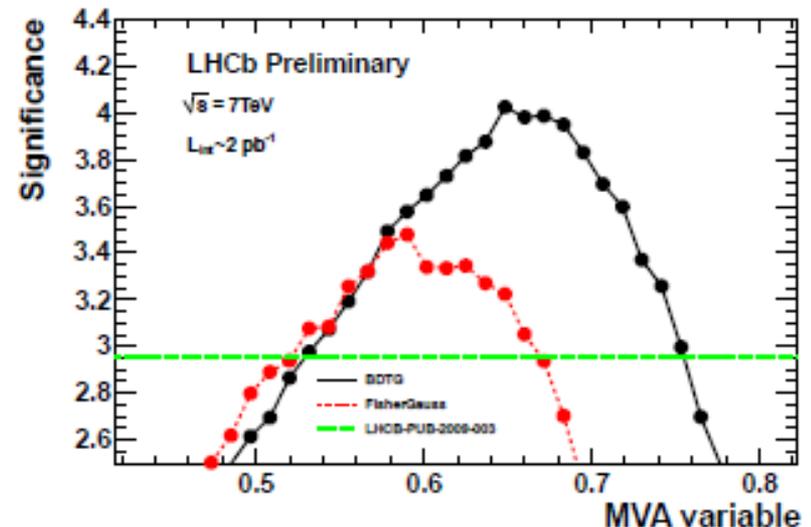
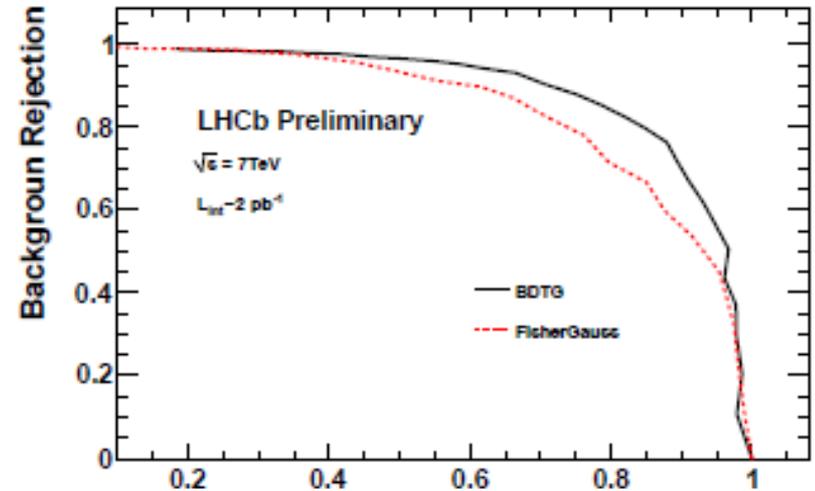
# Analysis strategy:



## Selection procedure

- ▶ Triggers and preselection the same for every signal mode – difference in the efficiencies arises due to  $B_s$  and  $B_d$  lifetime difference
- ▶ Offline selection
  - Using Gradient Boosted Decision Tree (BDTG) – one of MVA methods
  - Optimized for  $DK$  signal significance
  - Trained with  $2 \text{ pb}^{-1}$  of data, with Signal taken from the MC sample and background events from the  $B$  mass sidebands

Decay Channel	Efficiency
$B_d \rightarrow D\pi$	$75.5 \pm 0.8 \%$
$B_d \rightarrow DK$	$76.3 \pm 0.8 \%$
$B_s \rightarrow D_s\pi$	$75.2 \pm 0.4 \%$





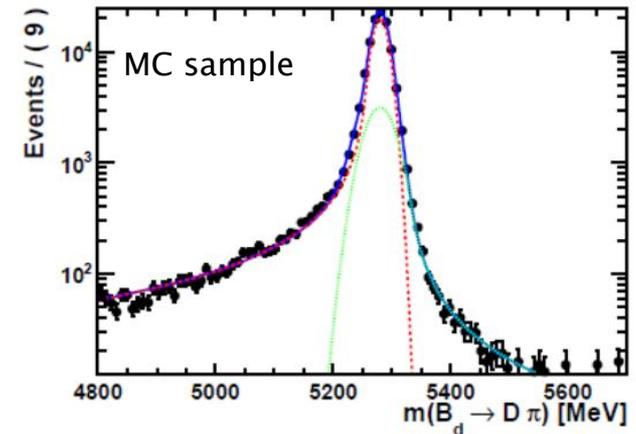
# Analysis strategy:

## Signal peak description



Double Crystal Ball function used for signal peak description

- Optimized using MC sample
- Left tail to account the radiative contribution
- Right tail to account non-Gaussian effects of the detector resolution



Parameter	$B^0 \rightarrow D^\pm \pi^\mp$	$B^0 \rightarrow D^\pm K^\mp$	$B_s^0 \rightarrow D_s^\pm \pi^\mp$	$B_s^0 \rightarrow D_s^\pm K^\mp$
Mean	$5280.47 \pm 0.06$	$5280.75 \pm 0.06$	$5367.61 \pm 0.04$	$5367.58 \pm 0.05$
$\alpha_1$	$1.79 \pm 0.02$	$1.82 \pm 0.03$	$1.56 \pm 0.01$	$1.70 \pm 0.01$
$\alpha_2$	$-2.08 \pm 0.04$	$-2.04 \pm 0.04$	$-1.74 \pm 0.07$	$-1.94 \pm 0.18$
$n_1$	$1.06 \pm 0.02$	$1.09 \pm 0.02$	$1.24 \pm 0.01$	$1.19 \pm 0.01$
$n_2$	$1.26 \pm 0.08$	$1.48 \pm 0.08$	$3.04 \pm 0.37$	$2.43 \pm 0.55$
$\sigma_1$	$14.22 \pm 0.15$	$13.29 \pm 0.16$	$12.99 \pm 0.05$	$12.28 \pm 0.10$
$\sigma_2$	$26.46 \pm 0.90$	$22.91 \pm 0.80$	$18.95 \pm 0.39$	$18.34 \pm 0.25$
Fract.	$0.79 \pm 0.02$	$0.73 \pm 0.02$	$0.59 \pm 0.02$	$0.55 \pm 0.01$

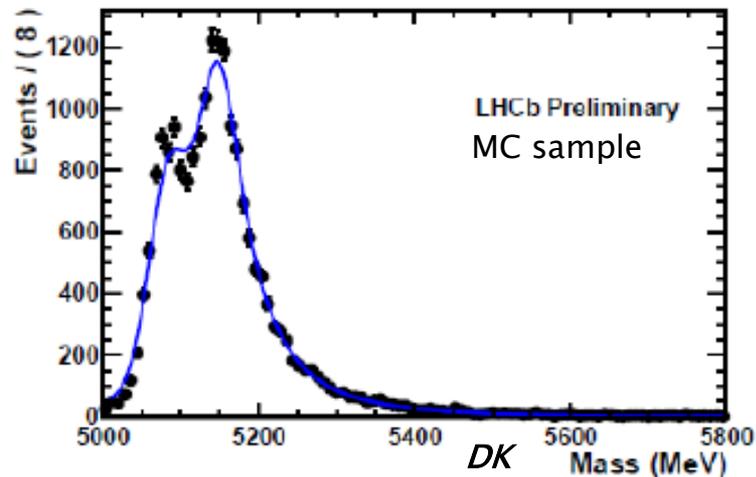
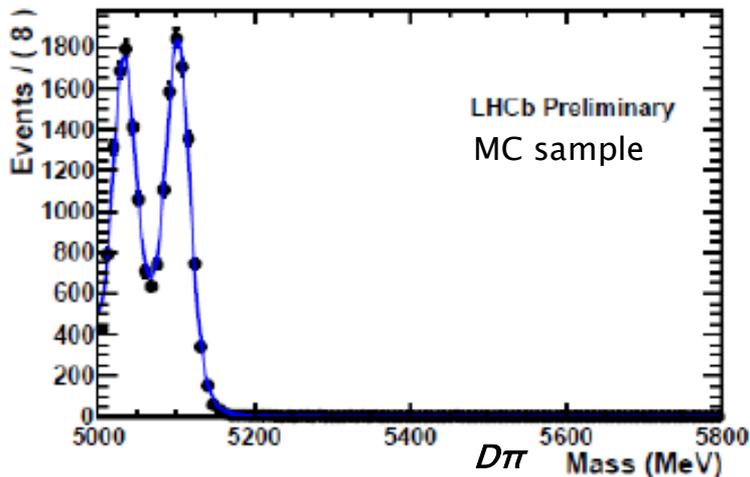


# Analysis strategy:

## Background description

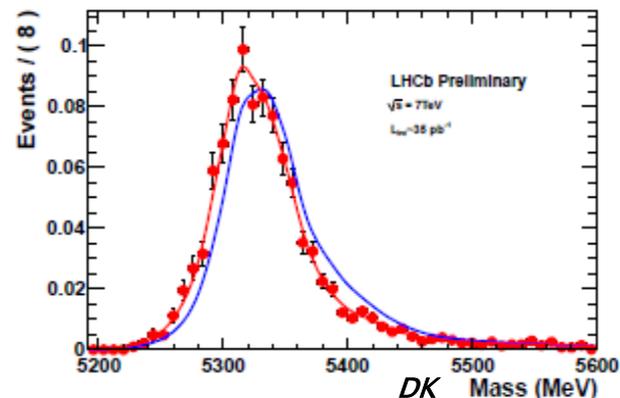
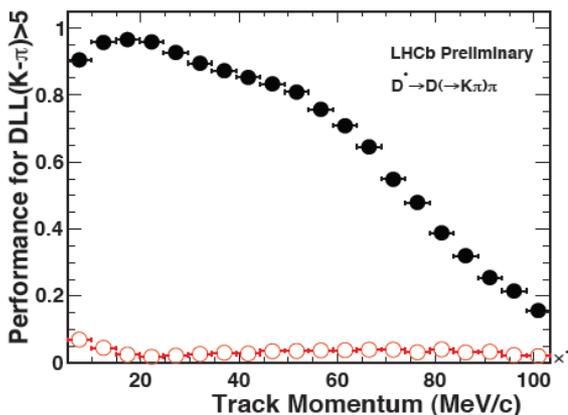
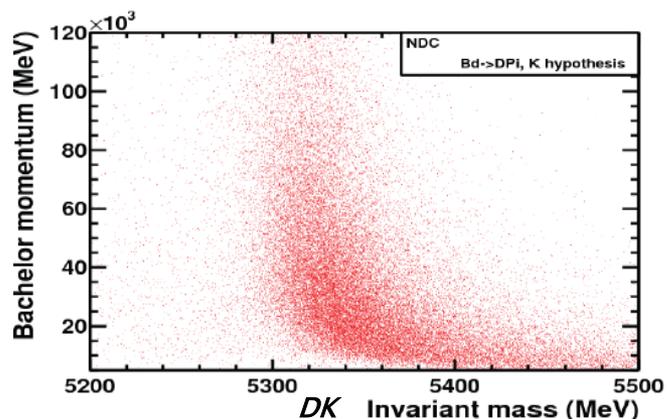


- ▶ Combinatoric background (prompt charm + pure combinatoric)
  - Single component describes with exponent/linear function (depends on the fitter)
- ▶ Partially reconstructed background e.g.:  $B_d \rightarrow D^* \pi$  with missing  $\pi^0$ 
  - Modelled with RooKeysPdf using MC samples
- ▶ Background from misidentification e.g.  $B_d \rightarrow D \pi$  with  $B_d \rightarrow DK$  mass hypothesis
  - Extracted from data using the reweighting procedure (see next slide)





# Analysis strategy: Reweight procedure

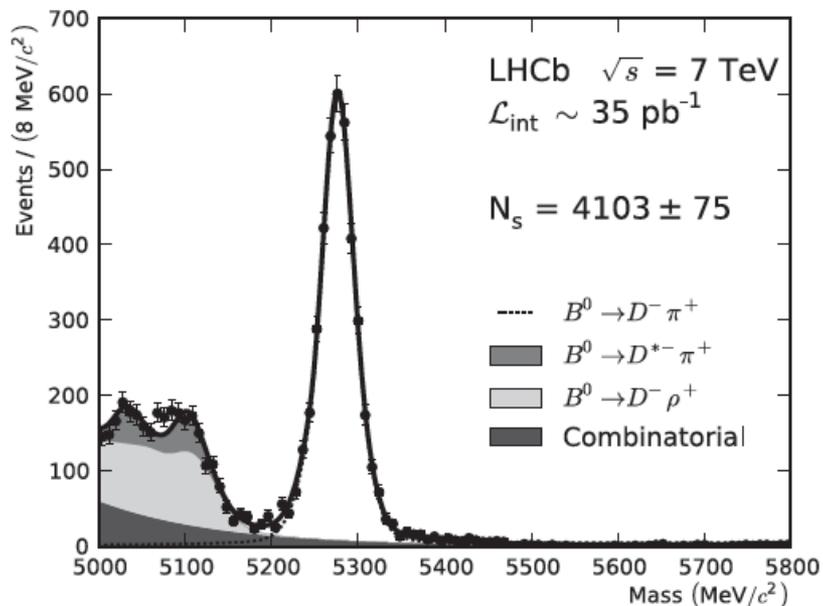


e.g.: Extracting  $B_d \rightarrow D\pi$  mass shape with  $B_d \rightarrow DK$  mass hypothesis:

1. Select 'pure'  $B_d \rightarrow D\pi$  sample under correct mass hypothesis
  2. Correct momentum distribution for the distortion caused by this cut
  3. Reweight according to the particle identification cut used for kaon bachelor selection
  4. Fix the kaon mass hypothesis with a RooKeysPdf
- Same procedure for all the mis-id backgrounds (e.g.  $B_s \rightarrow D_s\pi$ )



# Fit results – $B_d \rightarrow D\pi$



Parameter	Fitted value	Error
$N_{B^0 \rightarrow D^\pm \pi^\mp}$	4103	75
frac	0.58	0.06
mean	5276.3	0.4
$\sigma_1$	15.1	1.0
$\sigma_2$	27.1	1.2
$N_{Comb}$	1037	148
$a_1$	$-7.210^{-3}$	$0.510^{-3}$
$N_{D\rho}$	1631	198
$N_{D^*\pi}$	535	137

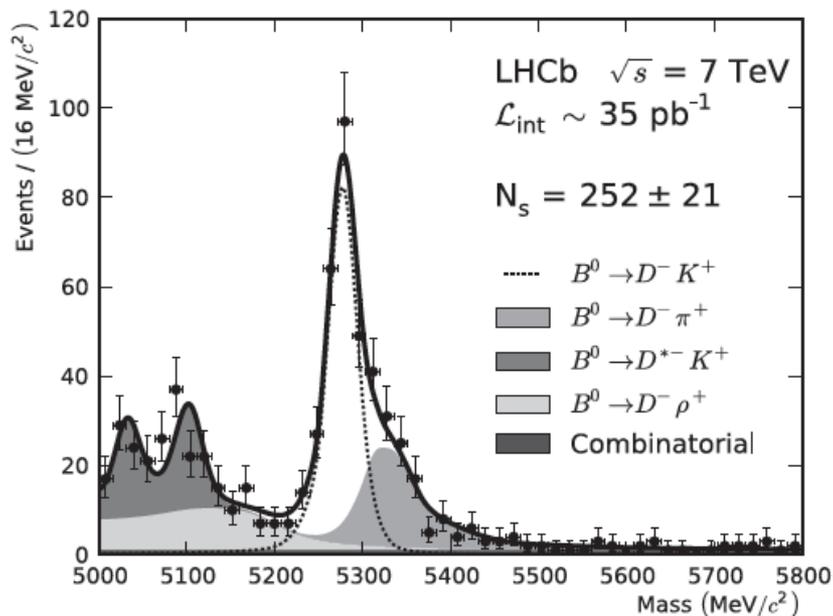
**$B_d \rightarrow D \pi :$   
 $4103 \pm 75$**

Signal  
Combinatorial  
Partially Reconstructed

- ▶ Using bachelor PID cut to rule out the  $B_d \rightarrow DK$  events
- ▶ All parameters free except the CB tails



# Fit results – $B_d^- \rightarrow DK$



**$B_d^- \rightarrow DK$  :**  
 **$252 \pm 21$**

Expected number of  $B_d^- \rightarrow D \pi$  (misID  $\pi \rightarrow K$ ): 142

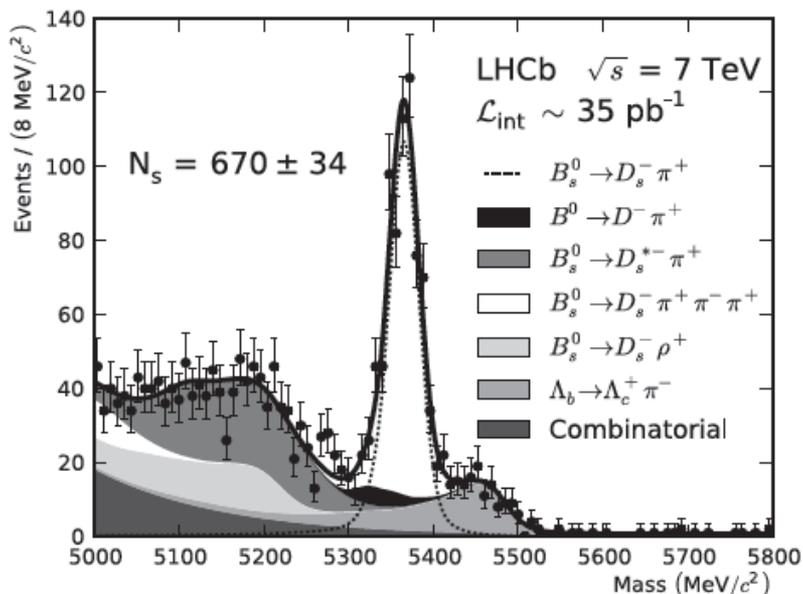
Parameter	Fitted value	Error
$N_{B^0 \rightarrow D^\pm K^\mp}$	252	21
frac	0.38	0.17
mean	5277.5	1.8
$N_{Comb}$	58	14
$N_{D\pi}$	131	19
$N_{D\rho}$	125	24
$N_{D^*K}$	123	19

Signal  
Combinatorial  
Partially Reconstructed

- ▶ Linear combintoric background
- ▶ Signal widths and CB tails are fixed



# Fit results – $B_s \rightarrow D_s \pi$



Expected number of  $B_d \rightarrow D \pi$  (misID  $\pi \rightarrow K$ ): 45

Parameter	Fitted value	Error
$N_{B_s^0 \rightarrow D_s^\pm \pi^\mp}$	670	34
$frac_{sg}$	0.50	0.14
mean	5365.3	1.0
$N_{Comb}$	345	240
$a_1$	$-6.610^{-3}$	$1.610^{-3}$
$N_{D\pi}$	48	18
$N_{\Lambda_b}$	287	36
$N_{B_s^0 \rightarrow D_s 3\pi}$	79	79
$N_{Part}$	668	121
$frac_{Part}$	0.34	0.06

- ▶ Linear combinatoric background
- ▶ Signal widths and CB tails are fixed
- ▶ Number of  $B_d \rightarrow D \pi$  events gaussianly constrained
- ▶ The  $B_s \rightarrow D_s^* \pi$  to  $B_s \rightarrow D_s \rho$  ratio constrained (ratio taken from the  $B_d \rightarrow D \pi$  fit results)

$B_s \rightarrow D_s \pi$  :  
 **$670 \pm 34$**



# Systematic uncertainty



Source	For $D_s^\pm \pi^\mp$ and $D^\pm K^\mp$	For $D_s^\pm \pi^\mp$ and $D^\pm \pi^\mp$
PID calibration	1.0%	2.5%
$B^0$ fit model	2%	2%
$B_s^0$ fit model	2%	2%
L0 Trigger efficiency	2%	2%
$D_s^\pm \rightarrow KK\pi$ B.R	4.9%	4.9%
$D^\pm \rightarrow K\pi\pi$ B.R	2.2%	2.2%
$\frac{\tau_{B_s^0}}{\tau_{B^0}}$	1.5%	1.5%
Correction factors	2.2%	2.2%
Total	7.0%	7.4%

- ▶ All systematic uncertainties strongly correlated
- ▶  $B_s \rightarrow D_s \pi / B_d \rightarrow DK$  more robust to PID systematics than  $B_s \rightarrow D_s \pi / B_d \rightarrow D \pi$



# Results



- ▶ Results of  $f_s/f_d$  with  
 $B_s \rightarrow D_s \pi / B_d \rightarrow DK$

and

$B_s \rightarrow D_s \pi / B_d \rightarrow D \pi$

$$\frac{f_s}{f_d} = 0.250 \pm 0.024^{\text{stat}} \pm 0.017^{\text{syst}} \pm 0.017^{\text{theor}}$$

$$\frac{f_s}{f_d} = 0.256 \pm 0.014^{\text{stat}} \pm 0.019^{\text{syst}} \pm 0.026^{\text{theor}}$$

- ▶ Combination of results:

$$\frac{f_s}{f_d} = 0.253 \pm 0.017^{\text{stat}} \pm 0.017^{\text{syst}} \pm 0.020^{\text{theor}}$$

- ▶ In agreement with leptonic measurements of the  $f_s/f_d$  ratio in LHCb
- ▶ In agreement with latest results from CDF and LEP
- ▶ Result published in [Phys. Rev. Lett. 107 \(2011\) 211801](#)
- ▶ Now aiming towards the CP measurements using those modes



Thank you

# Backup slides





# Trigger & Stripping



## Stripping cuts list

Parameter	Value
Global event cut	
Number of long tracks in the event	$\leq 180$
<i>D</i> selections	
$\chi^2/ndf$ for daughter tracks	$< 5$
$p_T$ for daughter tracks	$> 250 \text{ MeV}/c$
$p$ for daughter tracks	$> 2000 \text{ MeV}/c$
$\chi^2$ of daughter IP to PV	$> 4$
$\chi^2$ of IP to PV for at least one daughter	$> 40$ ,
Inv. mass window for <i>D</i> daughter combination	$\pm 110 \text{ MeV}/c^2$
Inv. mass window for <i>D</i> after vertex fit	$\pm 100 \text{ MeV}$
<i>D</i> vertex fit $\chi^2/ndf$	$< 12$
$p_T$ for <i>D</i>	$1500 \text{ MeV}$
<i>D</i> DIRA	$> 0.9$
DOCA between <i>D</i> daughter tracks	$< 1.5 \text{ mm}$
<i>B</i> selections	
Bachelor $p_T$	$> 500 \text{ MeV}/c$
Bachelor $p$	$> 5000 \text{ MeV}/c$
$\chi^2$ of bachelor IP to PV	$> 16$
<i>B</i> vertex fit $\chi^2/ndf$	$< 12$
$\chi^2$ of <i>B</i> IP to PV	$< 25$
<i>B</i> proper time	$> 0.2 \text{ ps}$
<i>B</i> DIRA	$> 0.9998$
Inv. mass window for <i>B</i> daughter combination	$\pm 500 \text{ MeV}/c^2$



# Selections



All particle momenta	$> 2000 \text{ MeV}$
All particle IP $\chi^2$	$> 9$
$D^\pm$ daughter $p_t$	$> 300 \text{ MeV}$
$D^\pm$ $p_t$	$> 2000 \text{ MeV}$
$D^\pm$ IP $\chi^2$	$> 9$
$D^\pm$ vertex $\chi^2$	$< 15$
$D^\pm$ FSPV ( $\chi^2$ )	$> 100$
$D^\pm$ mass	$(1870, 1969)_{-40}^{+24}$
Bachelor $p_t$	$> 500 \text{ MeV}$
$B^0$ vertex $\chi^2$	$< 10$
$B^0$ IP $\chi^2$	$< 16$
$B^0$ FSPV ( $\chi^2$ )	$> 144$
$B^0$ $\cos \theta$	$> 0.9999$

## Variables for BDTG



# Selections



$J/\psi K^*$  veto:

- ▶ No cut applied for D and B vertices separation thus small fraction of those can be reconstructed as  $D\pi$
- ▶ Two final state tracks satisfy „isMuon” criterion
- ▶ Mass of those tracks is in  $\pm 40\text{MeV}$   $J/\psi$  mass window

