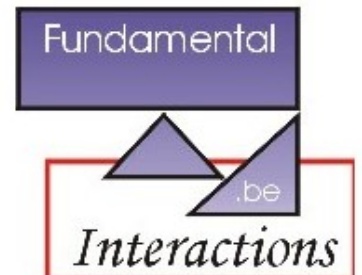


On high energy QCD factorization: theoretical basics and phenomenological applications

Krzysztof Kutak



(soon IFJ PAN)



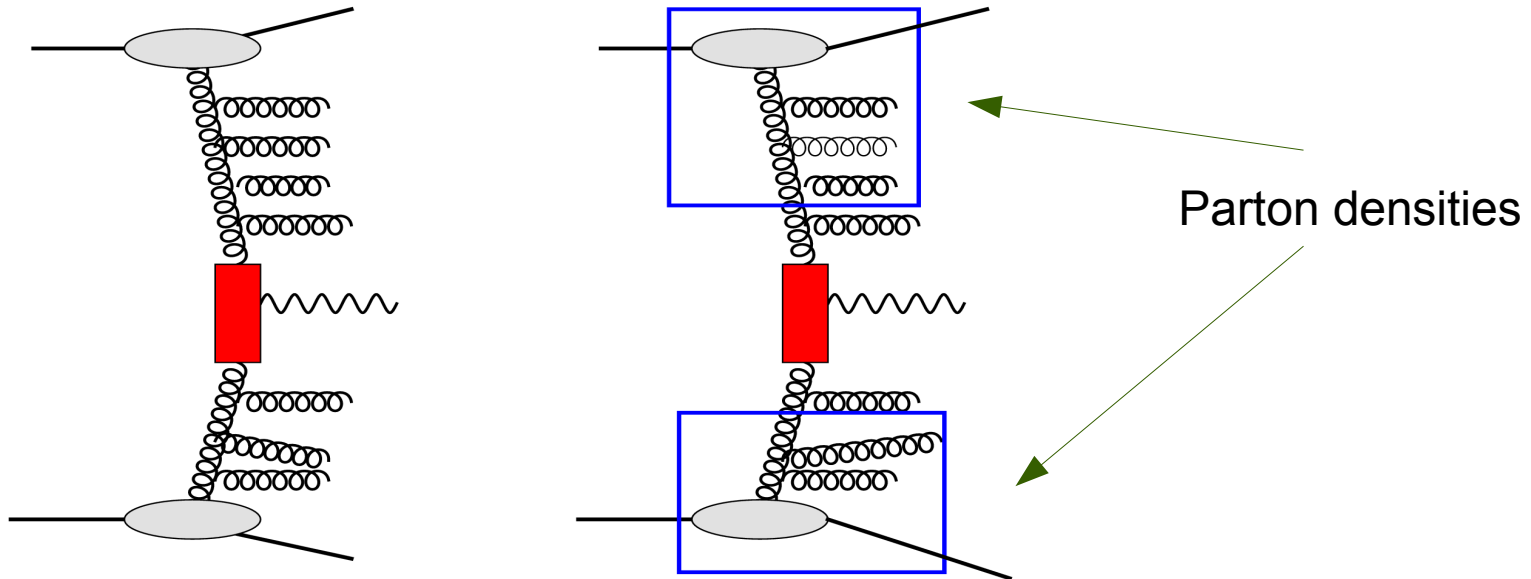
High energy scattering as a probe of new physics

- New dynamical effects in SM
Color Glass Condensate, Quark Gluon Plasma, saturation,...
- Production of new particles not included in SM
gravitons, SUSY, LED,...

To separate a “new physics signal” from the old background one needs to understand the behavior of QCD cross section at high energies (constraints, uncertainties of pdf sets, NLO calculations)

pQCD calculations

- Asymptotic freedom of QCD allows for perturbative calculations
 - Matrix element + factorization theorems
 - Factorization theorems allow for decomposition of process under some ordering condition into long and short distant parts (ep, pp, pA)



Matrix element convoluted with resummed contributions of higher orders -
Collinear Factorization , High Energy Factorization

$$\text{Observable} \sim \text{parton density} \otimes \text{ME} \otimes \text{parton density}$$

High energy factorization

Ciafaloni, Catani, Hautman '94

High energy factorization basic facts:

- gluon dominates (quark contributions neglected at LO)
- taking into account kinematics of the collision precisely enough at LO (takes into account some parts of NLO and NNLO of DGLAP)
- sums up large logarithms of energy
 - allows for formation of dense system which then saturates
 - implementation in Monte Carlo

$$L = -\frac{1}{4} F_{\mu\nu}^a F^{a,\mu\nu} + \text{source terms}$$

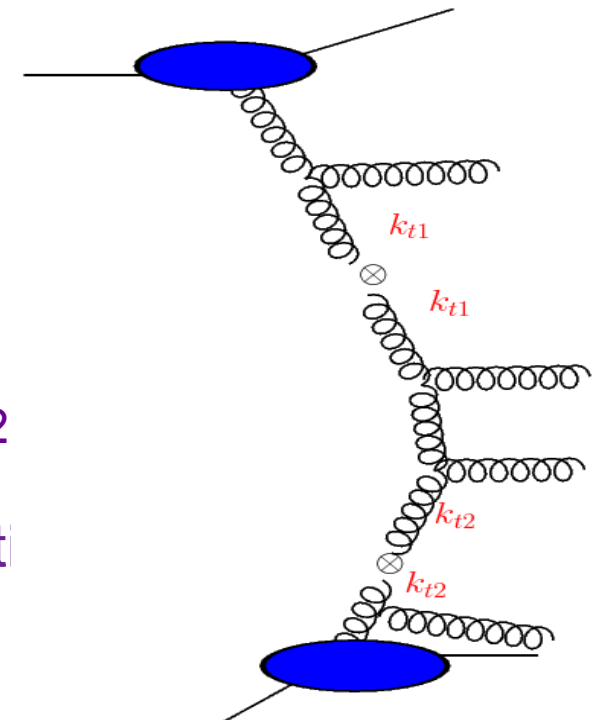
HIGH ENERGY LIMIT OF QCD

$$\sigma = \int dx_1 dx_2 d^2 k_{1T} d^2 k_{2T} f(x_1, k_{1T}) \hat{\sigma} f(x_2, k_{2T})$$

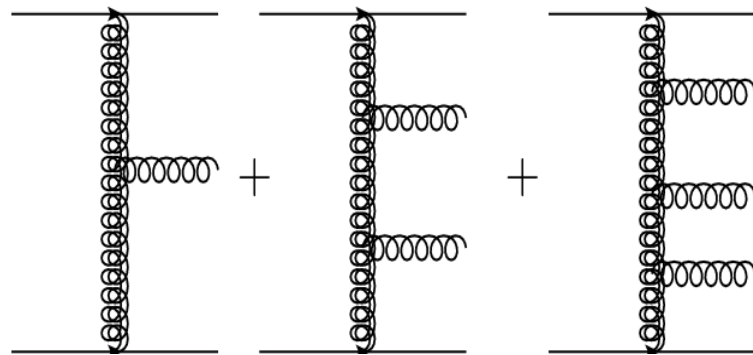
Ciafaloni, Catani, Hautman '90

Implemented in Monte Carlo generator CASCADE
(H. Jung)

- Parton density depends on k_t
 - Off shell initial state partons off shellness $\sim -k_t^2$
 - In collinear limit reduces to collinear factorizat



High energy limit of QCD basic equation: BFKL



$$+ \dots = \sum_n^{\infty} \ln^n s/s_0$$

$$\partial_Y f(Y, k^2) = K_{BFKL} \otimes f(Y, k^2)$$

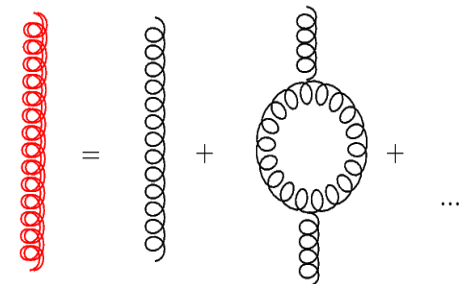
$f(x, k)$ - sum up diagrams -
s-square of total energy

$Y \sim \ln 1/x \sim \text{total energy}$

- Known also for SM YM
- Studied also in context of AdS/CFT
- Known up to NLO
- No hard scale: “evolution without observer”
- No useful Monte Carlo implementation

Balitsky Lipatov, Fadin, Kuraev '77

Reggeized gluon



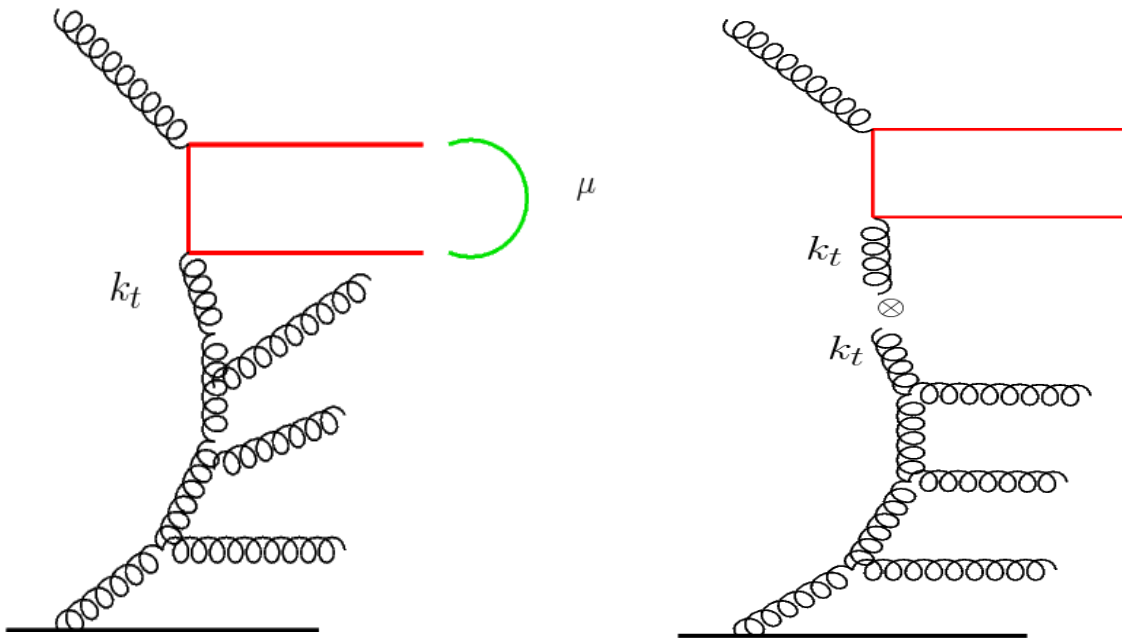
Valid for not too small $x \cdot 10^{-4}$

CCFM evolution equation - evolution with observer

- Linear equation based on strong ordering in angle
- Interpolates between DGLAP and BFKL
- Gluon density is build by constructive interference of gluons
- Sumes up also logs of hard scale

$$\mathcal{A}(x, k_t^2, \mu) = K_{CCFM} \otimes \mathcal{A}(x, k_t^2, \mu)$$

Catani, Fiorani, Marchesini '90

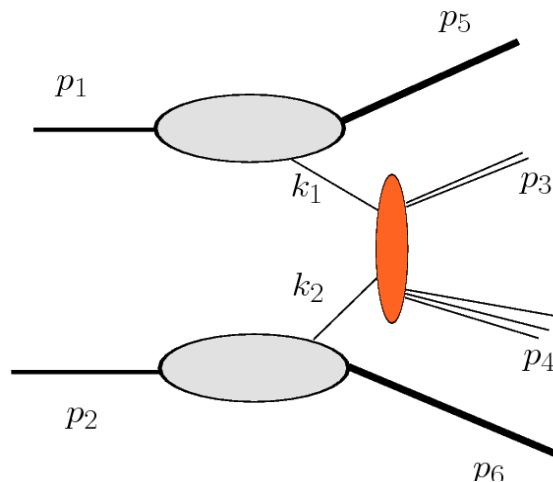


Implemented by H. Jung in
Monte Carlo CASCADE

High energy factorization and forward jets

$$\frac{d\sigma}{d^2p_{t1}d^2p_{t2}dy_1dy_2} = \sum_a \int d^2k_t \phi_{a/A}(x_1, \mu) \otimes |M|^2 \otimes \phi_{g^*/B}(x_2, k_t^2, \mu)$$

Consistent resummation both logs of rapidity and logs of hard scale



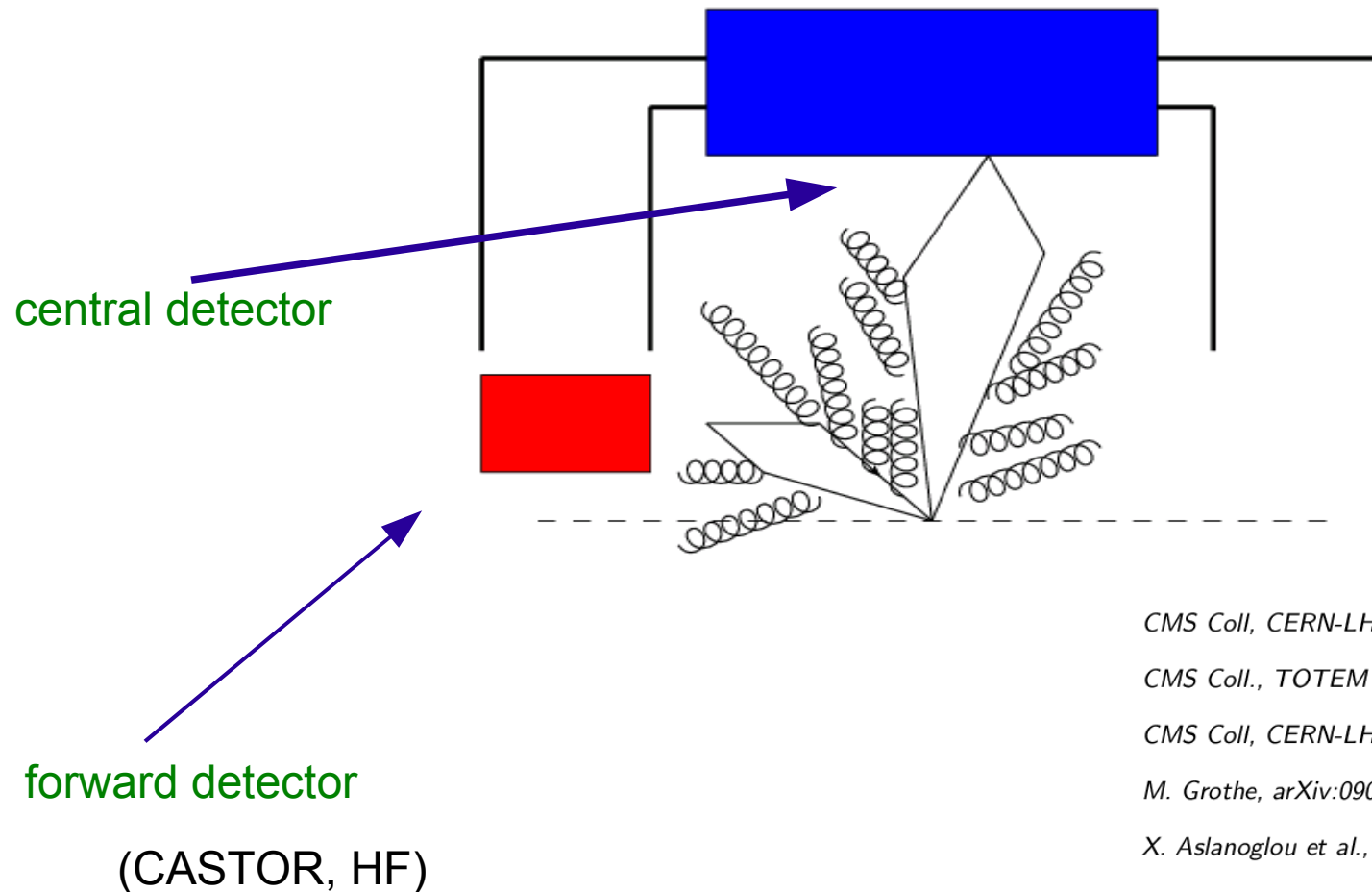
Deak, Jung, Hautmann & Kutak '09

Knowing well parton densities at large x one can get information about low x physics

- ◇ ϕ_a near-collinear, large- x ; ϕ_{g^*} $k_\perp$ -dependent, small- x
- ◇ $\hat{\sigma}$ off-shell continuation of hard-scattering matrix elements

Measurement

- Polar angles small but far enough from beam axis
 - Measure: spectra of jets, angular correlations



CMS Coll, CERN-LHCC-2006-001; CMS PAS FWD-08-001 (2008);

CMS Coll., TOTEM Coll, CERN-LHCC-2066-039/G -124 (2006)

CMS Coll, CERN-LHCC-2006-001; CMS PAS FWD-08-001 (2008);

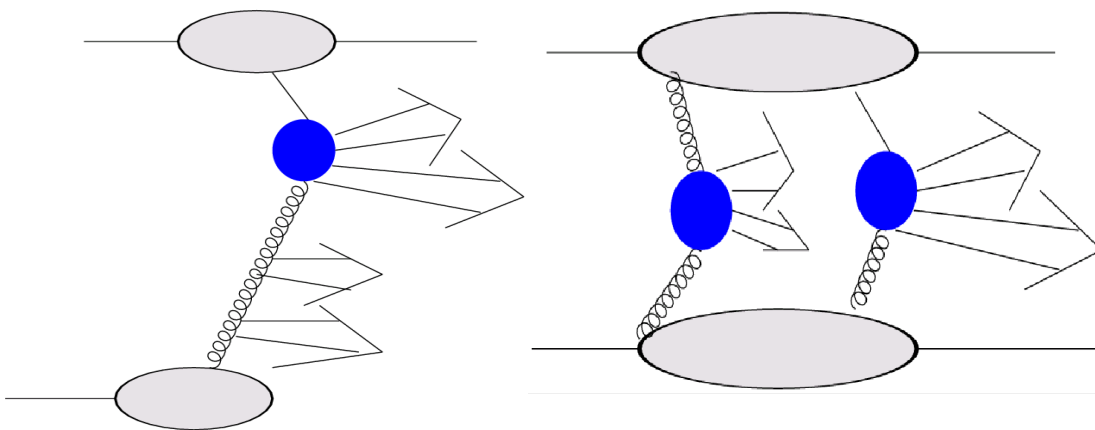
M. Grothe, arXiv:0901.0998; D. d'Enterria, arXiv:0806.0883;

X. Aslanoglou et al., CERN-CMS-NOTE-2008-022 (2008)

H. Jung et al., HERA-LHC Proc. arXiv:0903.3861;

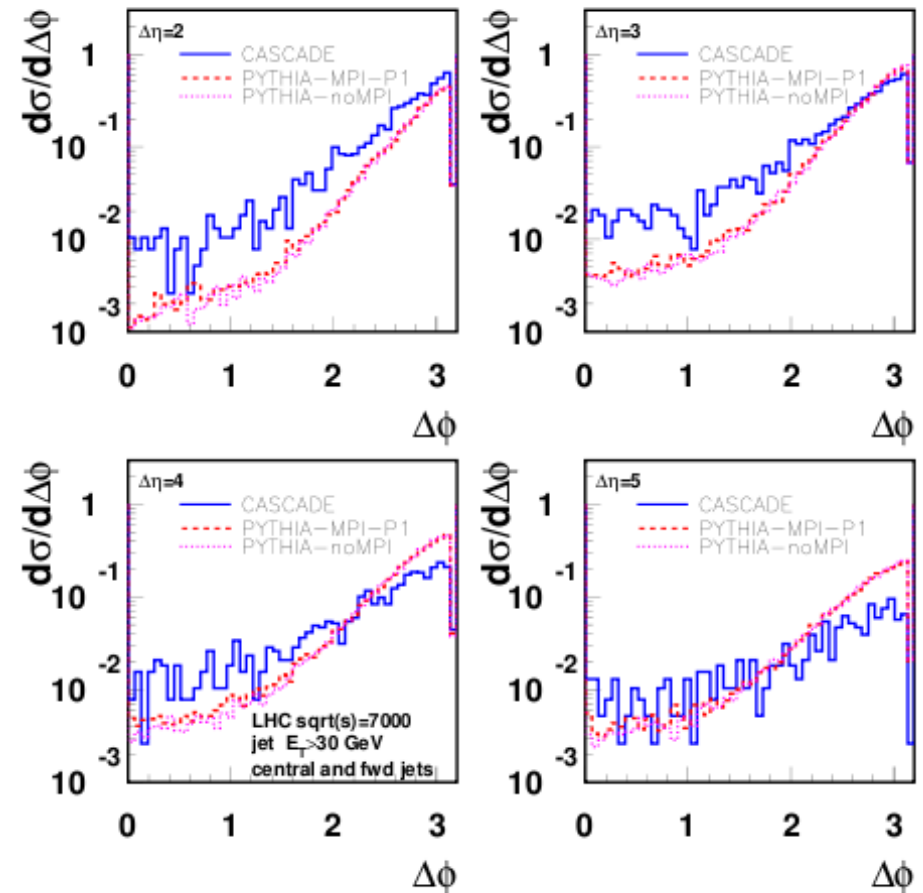
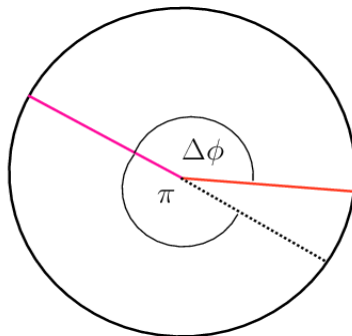
Cross section as a function of the azimuthal difference for different rapidities

Deak, Jung, Hautmann, Kutak '10



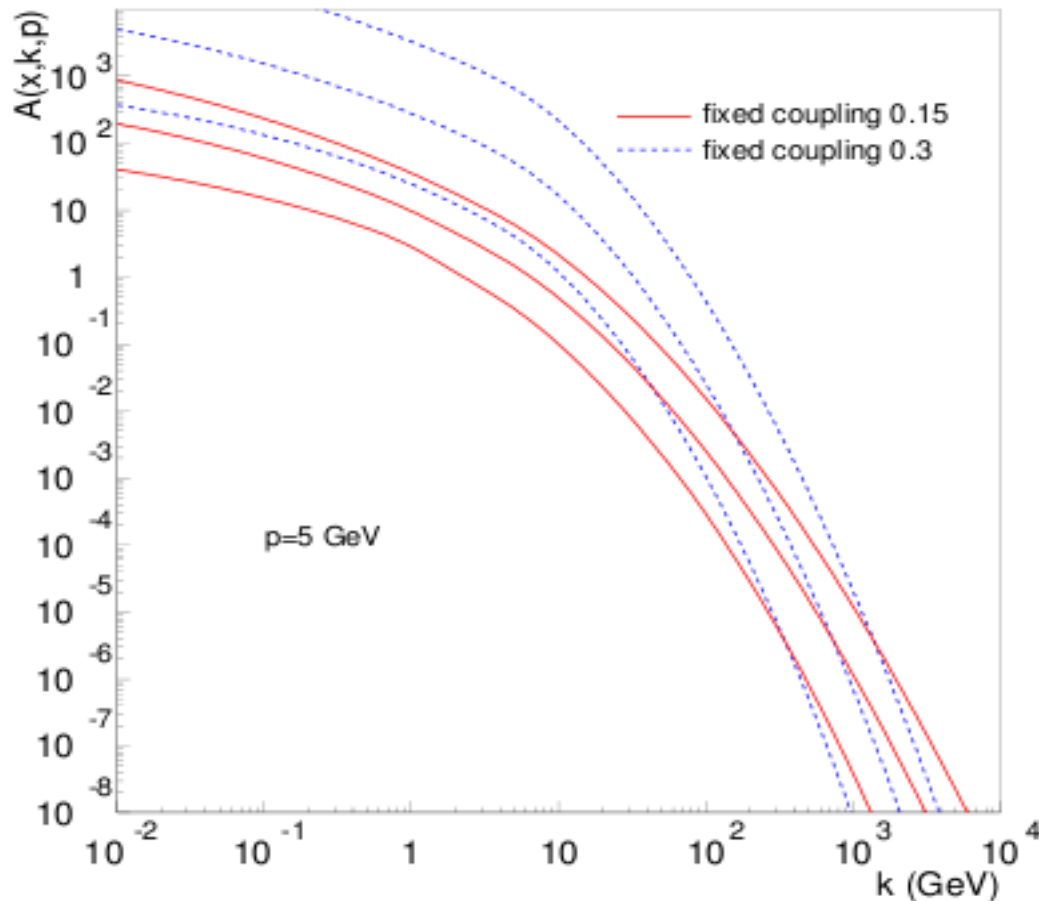
Single chain

Multiple interactions



- Observable which measures jet activity in the parton shower
 - Noticeable differences between different approaches

Towards dense partonic system and saturation



From Avsar, Stasto '10

$$\sigma_{\text{tot}} \stackrel{E \rightarrow \infty}{\leq} \ln^2 E$$

BFKL and CCFM are linear and predict strong growth of number of gluons. The growth has to be stopped.

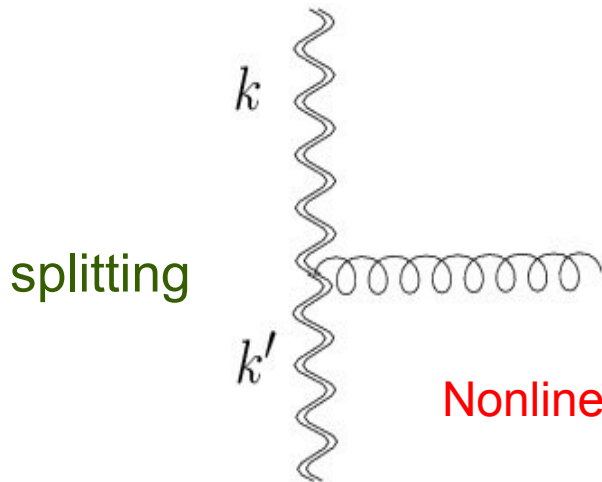
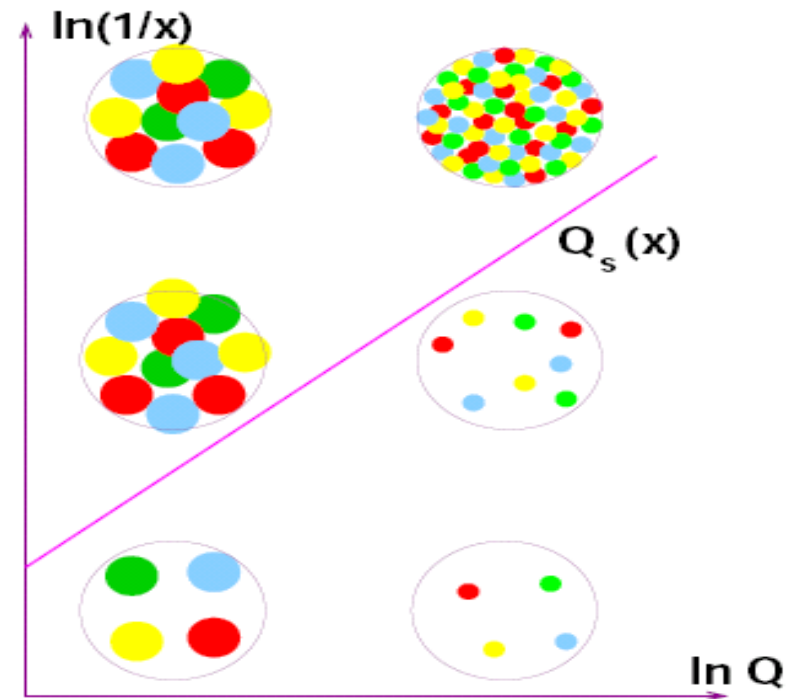
High energy factorization and saturation

Saturation – state where number of gluons stops growing due to high occupation number

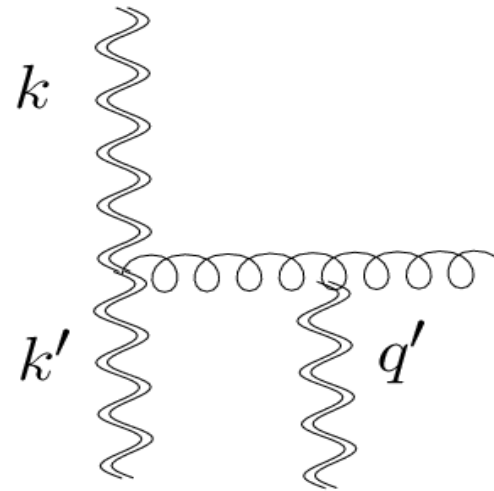
Cross sections change their behaviour from power like to **logarithmic like**.

Gribov, Levin, Ryskin '83

On microscopic level it means that gluon apart from



recombination

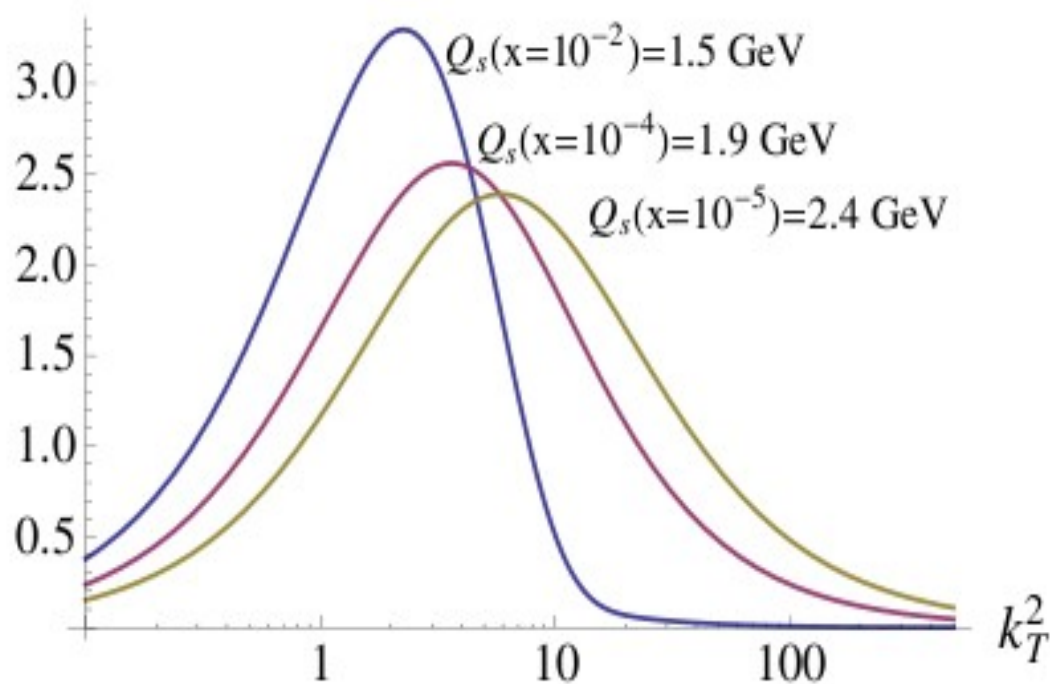


Nonlinear evolution equation BK

Balitsky, Kovchegov

PROPERTIES OF GLUON DENSITY

Saturation allows to define well mean number of gluons and mean momentum



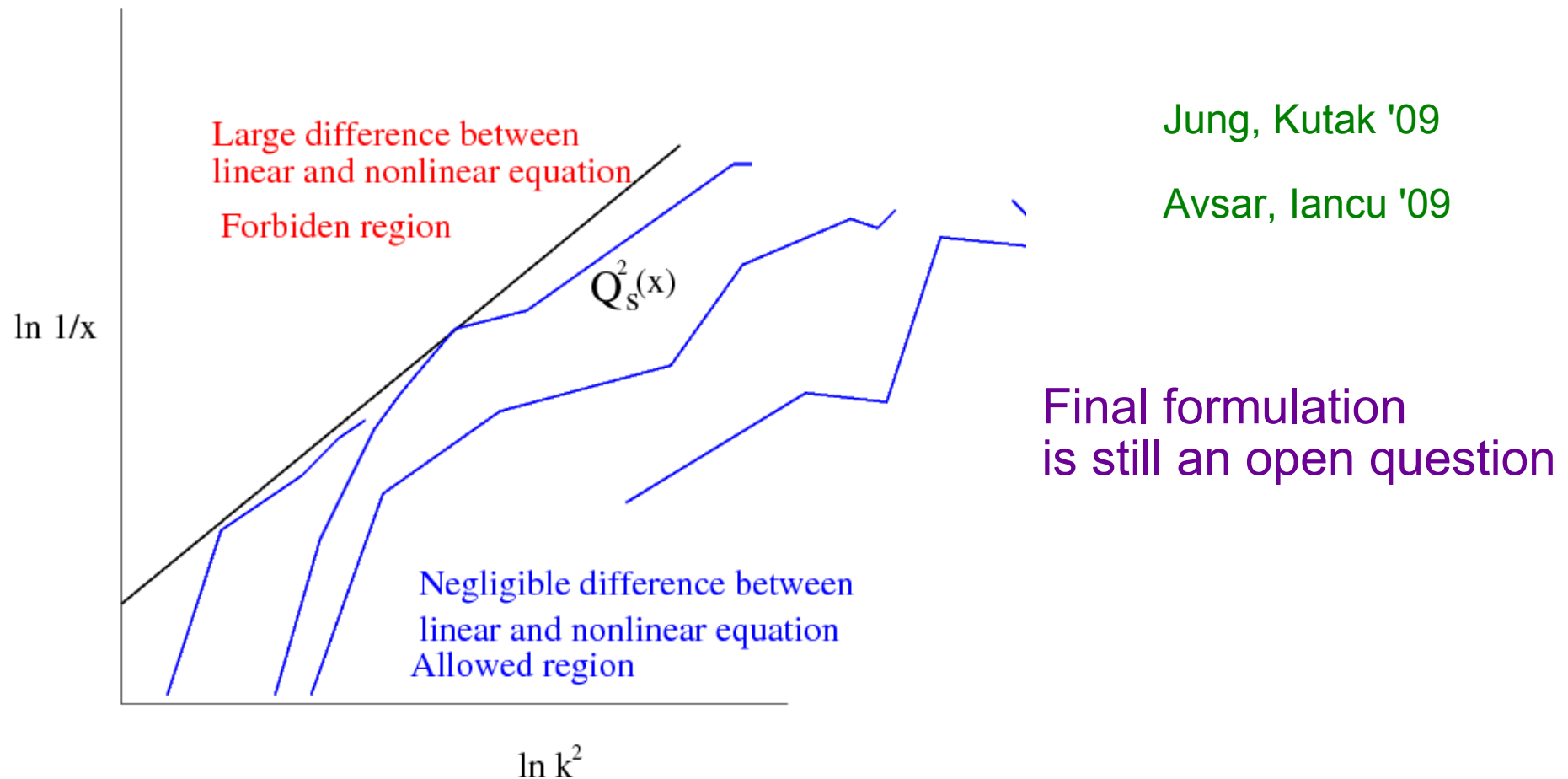
$$\langle k_t^2 \rangle \sim Q_s^4(x)$$

$$\langle n \rangle \sim Q_s^2(x)$$

Saturation scale.
Most gluons have momentum
of order of saturation scale

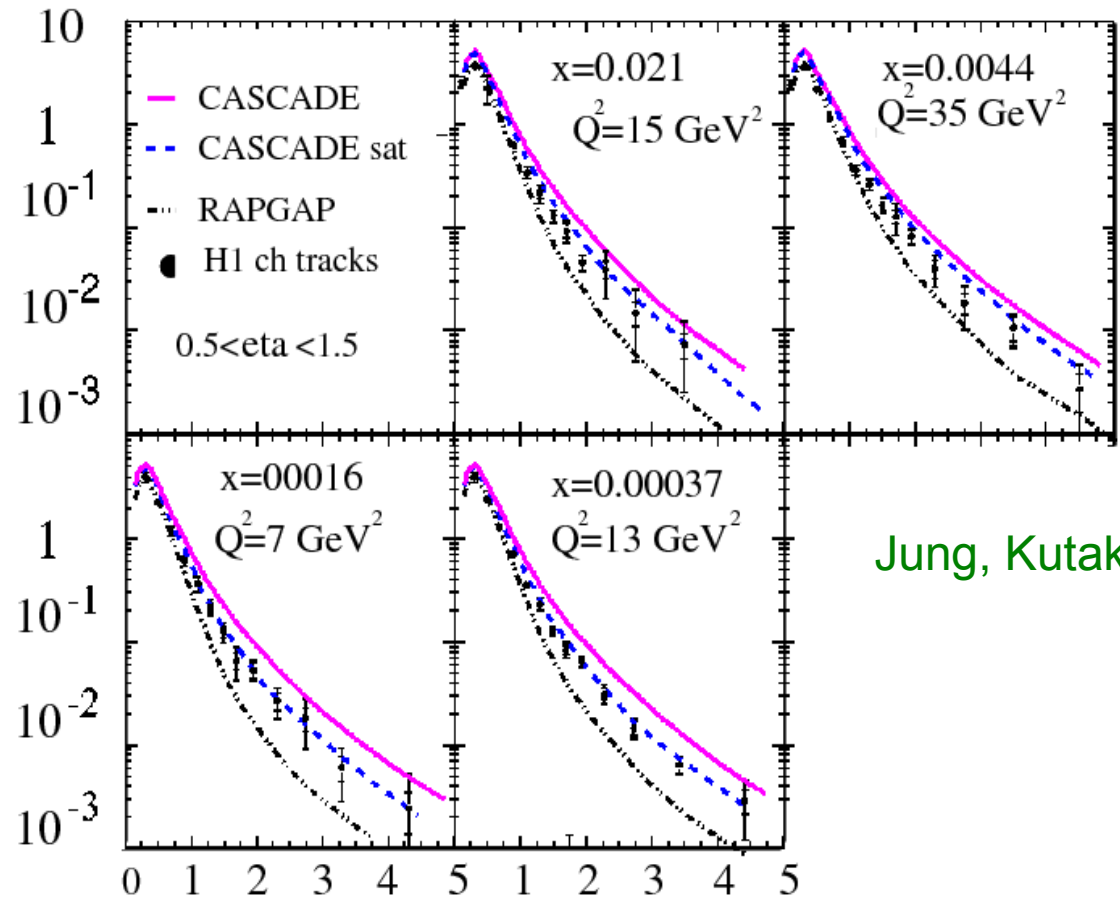
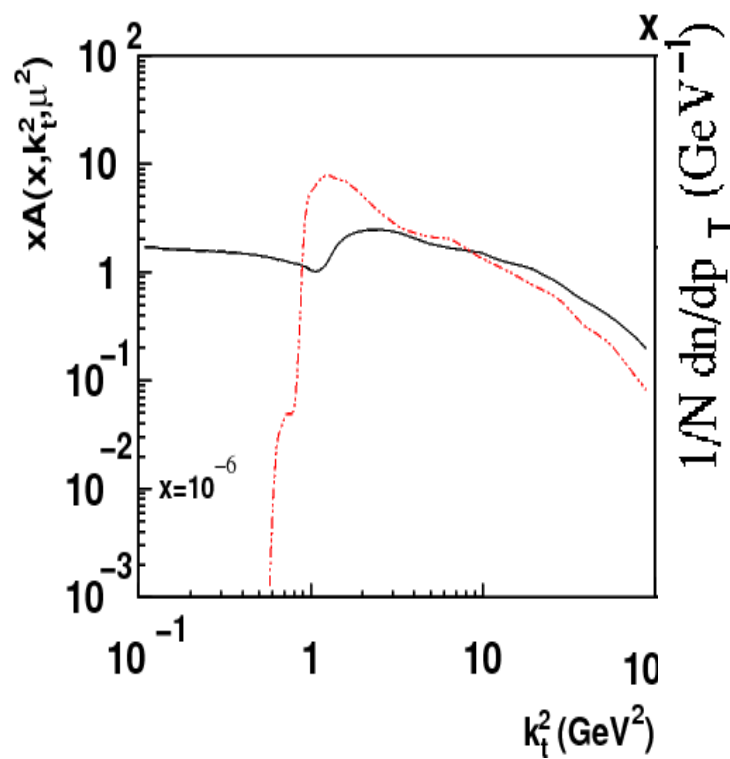
Solution of BK equation

CCFM with saturation – first steps



- Introduce line which will introduce effectively saturation effects in evolution.
- Trajectories which enter the saturation region are rejected.

CCFM with saturation – first steps



Jung, Kutak '09

- Gluon density suppressed at low k .
 - This affects pt distribution of charged particles

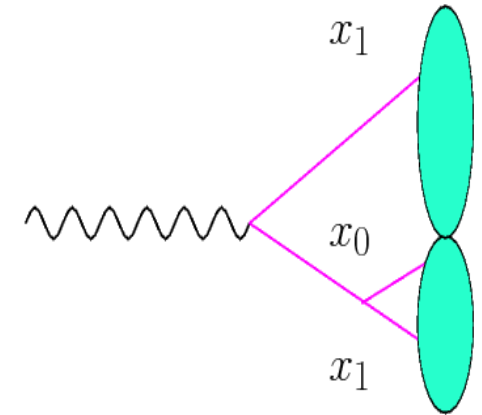
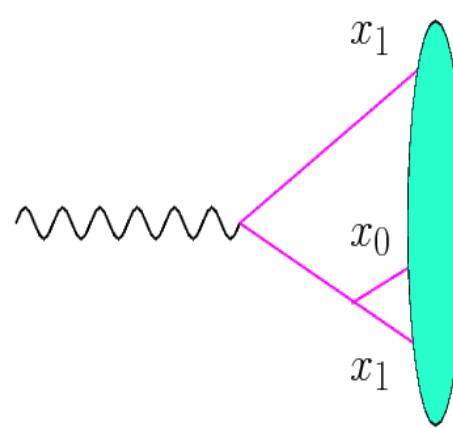
High energy factorization and Color Glass Condensate

McLerran, Venugopalan, Iancu, Leonidov, Weigert, ...

Colour: The gluons are coloured

Glass: Slow evolution of associated fields

Condensate: Very high density of massless gluons



$$\frac{\partial}{\partial Y} \langle \mathcal{D}_{01} \rangle = \frac{g^2}{8\pi^3} \int d^2 x_2 [\langle \mathcal{D}_{02} \mathcal{D}_{21} \rangle - N_c \langle \mathcal{D}_{01} \rangle] K_{021}$$

$$\begin{aligned} \langle \mathcal{D}_{02} \rangle &= d_{02} \\ \langle \mathcal{D}_{02} \mathcal{D}_{21} \rangle - \langle \mathcal{D}_{02} \rangle \langle \mathcal{D}_{21} \rangle &= d_{0221} \end{aligned}$$

+ infinite number of equations for correlators of higher order

JIMWLK, Balitsky chain

$$K_{021} = \frac{x_{01}^2}{x_{02}^2 x_{21}^2}$$

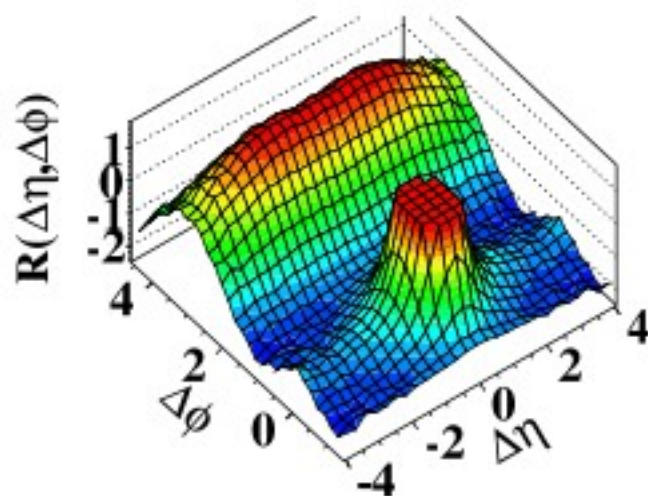
Practical calculations in Color Glass Condensate

make use of expansion of correlators in terms

of gluon density obtained from high energy factorisation

Color Glass Condensate and high multiplicity events in pp collision at LHC

CMS '10



Ridge-like structure of correlated charged particles pairs with momenta in the range $q_t, p_t, 1-3$ GeV.

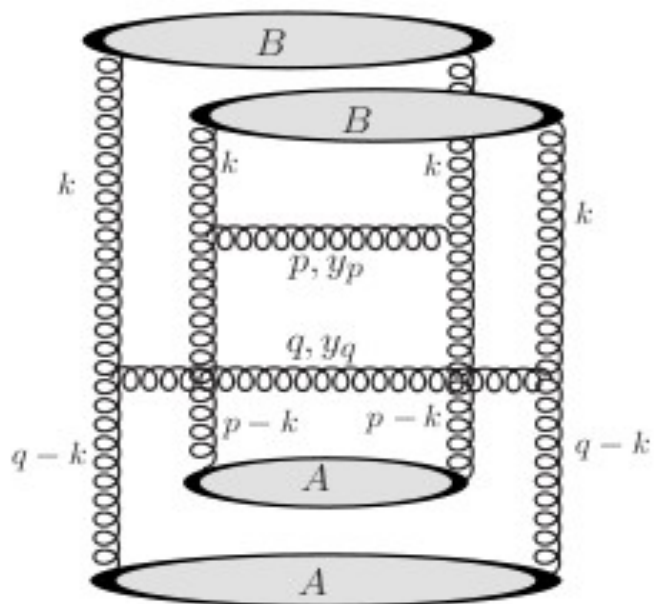
Not really expected in pp. Similar objects are showing up in AA collision due to elliptic flow- signature of collective expansion. Subleading for pp – not so dense system

Possible explanations:

- momentum conservation (P. Van Mechelen; P. Bozek '10)
 - CGC effects in pp – correlation in production on distances $1/Q_s$ and existence of maximum of gluon density selects:

$$|\mathbf{p}_\perp - \mathbf{k}_\perp| \sim Q_s \quad |\mathbf{q}_\perp - \mathbf{k}_\perp| \sim Q_s$$

Dumitru et. al. '10



Conclusions

- LHC opens phase space for large center-of -mass energies and for presence of multi-scales
 - Already we have exciting new results from LHC
 - Many, new challenging issues ahead