$\Theta^{+}(1540)$ and Associated Exotic States

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Based on work in collaboration with R. Arndt, Ya. Azimov, M. Polyakov, R. Workman

Epiphany2005, Jan 6-8, 2005

Outline

- Prehistory of exotics
- What we know about $\Theta^{\scriptscriptstyle +}$
- How to search for alternatives ? Modified PWA
- Θ^+ (non)observation
- Kinematic reflections
- Is N* = N(1710)?
- Theoretical expectation
- Experimental evidences for N*
- Summary

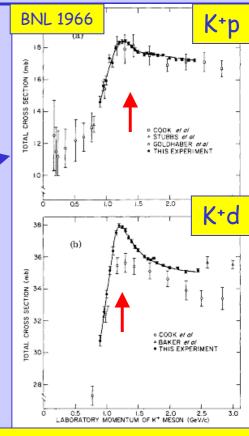
Prehistory of Exotics

- The problem of observing multiquark (exotic and/or `cryptoexotic') states is as old as quark themselves
- The first experimental results on search for baryon exotics in KN system

[R. Cool *et al*, Phys Rev Lett **17**, 102 (1966)
R. Abrams *et al*, Phys Rev Lett **19**, 259 (1967)
J. Tyson *et al*, Phys Rev Lett **19**, 255 (1967)]

were published soon after the invention of quarks

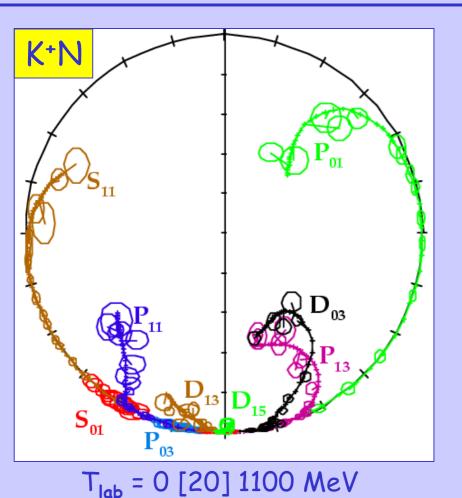
[M. Gell-Mann, Phys Lett **8**, 214 (1964) G. Zweig, CERN preprints TH-401, TH-412, 1964



 Resonance peak found in K⁺N at M = 1910 MeV, Γ = 180 MeV

Standard PWA for K⁺N

[J. Hyslop, R. Arndt, D. Roper, R. Workman, Phys Rev D 46, 961 (1992)]



- One of the most convincing way to search for ⊕⁺ is PWA
- Pole Positions:

Ι	Ampl	ReW	-ImW	
	·	(MeV)	(MeV)	
0	P ₀₁	1831	95	+
	D ₀₃	1788	170	
1	P ₁₃	1811	118	
	D ₁₅	2074	253	

 All suggested resonances are too heavier than known
 O⁺ to be its isospin partners

Θ^+ and $\Phi - What$ is known [PDG (S. Eidelman *et al*) Phys Lett B **592**, 1 (2004)]

	Experiment	Mass (MeV)	Width (MeV)	
Θ(1540)⁺	LEPS	1540 ± 10	<25	
	DIANA	1539 ± 2	< 9	
	CLAS (d)	1542 ± 5	<21	
	SAPHIR	$1540\pm4\pm2$	<25	Only one pw P ₀₁ admits the effect at 1540 - 1450 MeV
	ITEP (v)	1533 ± 5	<20	with $\Gamma < 1$ MeV
	CLAS (p)	1555 ±10	<26	[R. Arndt, IS, R. Workman, Phys Rev C 68 , 042201 (2003)]
	PDG average	1539.2 ± 1.6	- /	
	GWU	1545	≤1	With additional
	LBNL	1540	0.9±0.3	assumption and unknown systematics
Ф(1860)	NA49	1862±2	<18	[R. Cahn and G. Trilling, PRD 69 , 011501 (2004)]
		<mark>s similar to expec</mark> M. Polyakov, Z Ph		

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Narrow Resonances in PWA

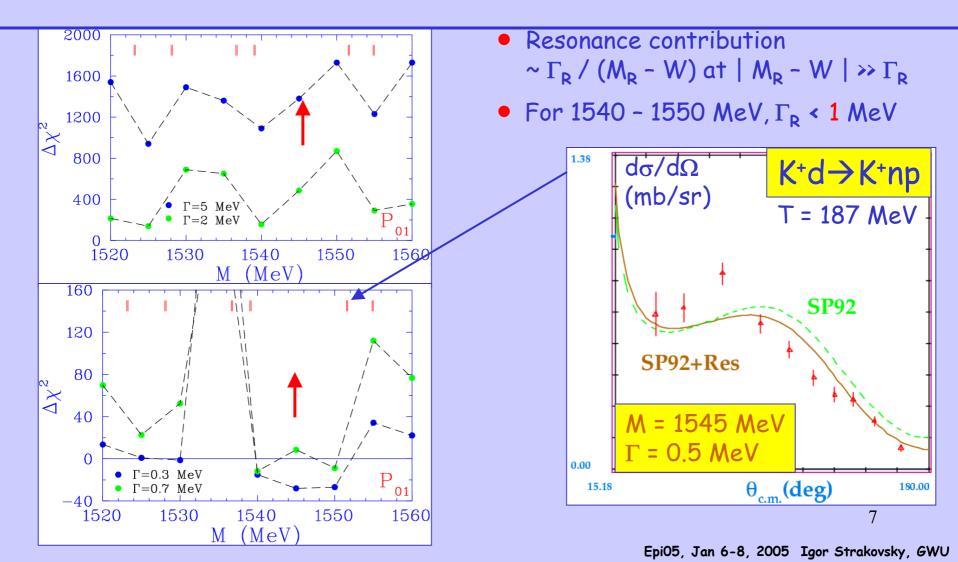
[R. Arndt, Ya. Azimov, M. Polyakov, IS, R. Workman, Phys Rev C 69, 035208(2004)]

- Standard PWA reveals only wide resonances ($\Gamma < 500 \text{ MeV}$)
- PWA (by construction) tends to miss resonances with Γ < 30 MeV
- We assume the existence of a Res and refit over the whole database
- Insertion of narrow resonances in PWA for elastic case: $e^{2i\delta} \Rightarrow e^{2i\delta}_{R} e^{2i\delta}_{B}$ $e^{2i\delta}_{R} = (M_{R} - W + i\Gamma_{R}/2)/(M_{R} - W - i\Gamma_{R}/2)$

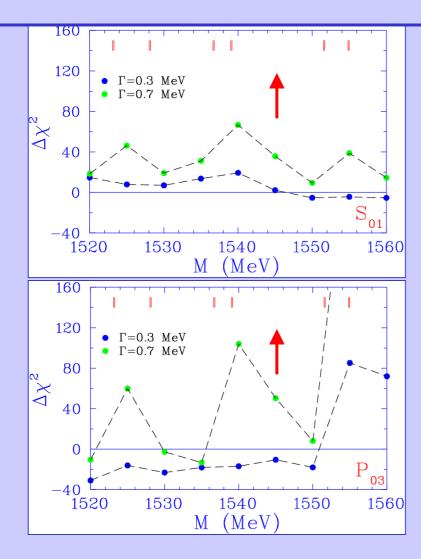
$$\begin{array}{l} \text{inelastic case: } \eta \ e^{2i\delta} \Rightarrow \langle a|S|a \rangle = r_a \ A(W) \ e^{2i\delta}_R + (1 - r_a) \ B(W) \\ r_a = BR(R \rightarrow a) \qquad |A(M_R)| = 1 \qquad \Sigma r_a = 1 \\ \eta \leq 1 \Rightarrow \ r_a \ |A(W)| + (1 - r_a) \ |B(W)| \leq 1 \end{array}$$

• How does this insertion changes χ^2 ? (Will it decrease ?)

$\Delta \chi^2$ due to Insertion of a Res into $P_{01}(J^P = \frac{1}{2})$



Check other Partial Waves

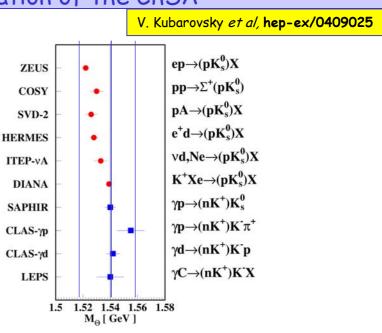


• $\Delta \chi^2$ due to insertion of a resonance into S₀₁ (J^P = 1/2⁻)

• $\Delta \chi^2$ due to insertion of a resonance into P₀₃ (J^P = 3/2⁺)

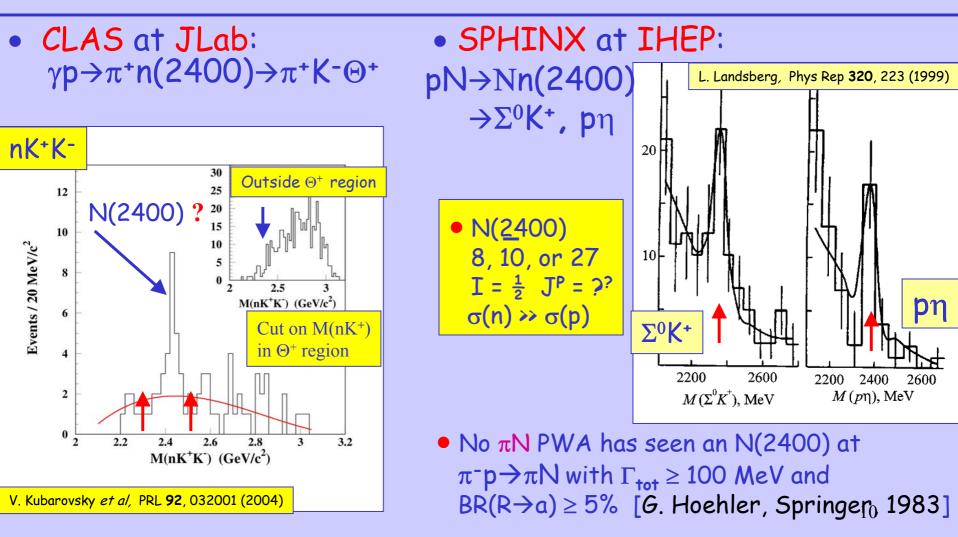
Summary on Exotic Baryon Observation

- The measured Mass looks similar to expectation of the ChSA
- The measured Width is only upper limit
- Highest Significance (CLAS) = 7.8σ
- Spin and Parity are not measured yet
- Production Mechanisms are unknown
 - Xsections are uncertain
 - NA49 results yet to be confirmed
 - Search for the other Flavor Partners is underway
 - CLAS fans, please be patient, g10 (*10) and g11 (*15) data are coming soon



• LEPS (*5), DIANA (*2), and COSY-TOF (*5) data are coming as well

Possible Mechanism of Θ^+ Production, N(2400) [Ya. Azimov, IS, Phys Rev C 70, 035210 (2004)]

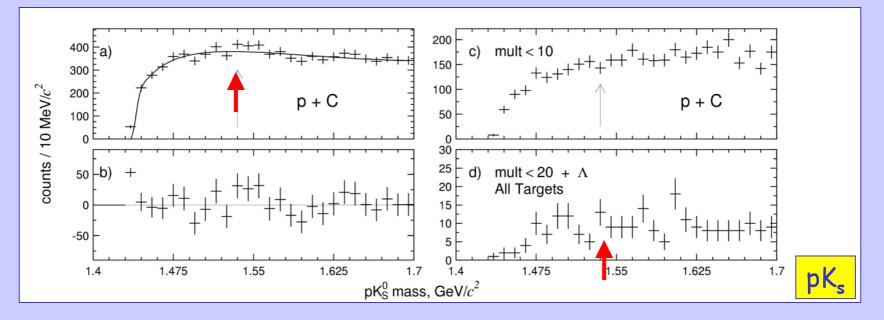


(Non)observation of Θ^+ (?)

- What we can learn from published High Energy (non)observations of Θ⁺?
- HERA-B in pA at $\sqrt{s} = 41.6 \text{ GeV}$
- **PHENIX** in dA at $\sqrt{s} = 200 \text{ GeV}$
- **BES** in e^+e^- at J/ψ and $\psi(2S)$
- plus several more measurements

• HERA-B [K. Knoepfle *et al,* J Phys G 30, S1363 (2004)]

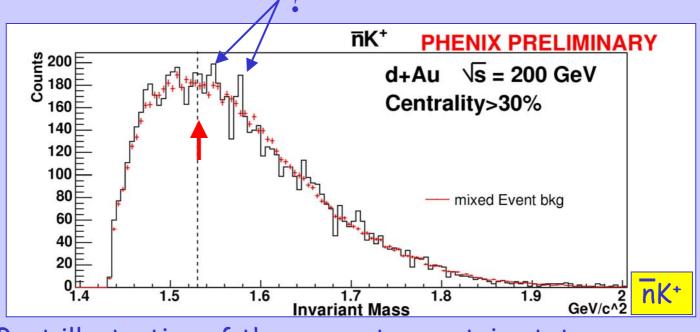
 Some features of data suggest a small ⊕⁺ signal with very large background. Special selection(s) may be needed



• Still hint at a possibility to extract a Θ^+

• **PHENIX** [C. Pinkenburg *et al*, J Phys G **30**, S1201 (2004)]

 The Quark Matter 2004 talk with `clear O' signal' transformed into the Proceedings text with `no signal' after a `small correction'. The situation is not clear even to the authors.



• Best illustration of the present uncertain status

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BES [J. Bai *et al*, Phys Rev D 70, 012004 (2004)]
 Analysis [Ya. Azimov, IS, Phys Rev C 70, 035210 (2004)]

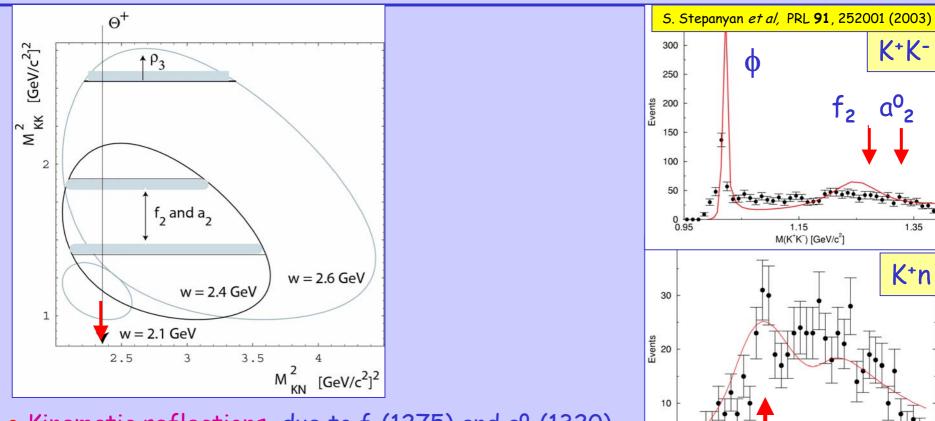
- Data need some (rather soft) dynamical suppression, say
 1/5 in the probability
- Meanwhile, because of necessity to produce directly two more qq pairs (in exotic decays as compared with decays to canonical baryon-antibaryon pairs), some dynamical suppression should naturally arise
 One or two order suppression might be quite natural
- Thus, the recent result of BES is only a starting point for investigating exotics in e⁺e⁻-annihilation

Summary on Θ^+ (non)observation

- Different initial particles
- Different energies
- Different production mechanisms
- How to separate ?
- Published `Null' Experiments do not really contradict the existence of pentaquarks; need to (im)prove their sensitivity

Kinematic Reflections

[A. Dzierba et al, Phys Rev D 69, 051901 (2004)]



- Kinematic reflections due to $f_2(1275)$ and $a_2^0(1320)$ can generate a narrow enhancement in K⁺n eff mass
- Fluctuations of the broad peak could result in a false narrow structure

1.6

M(nK⁺) [GeV/c²]

1.7

16

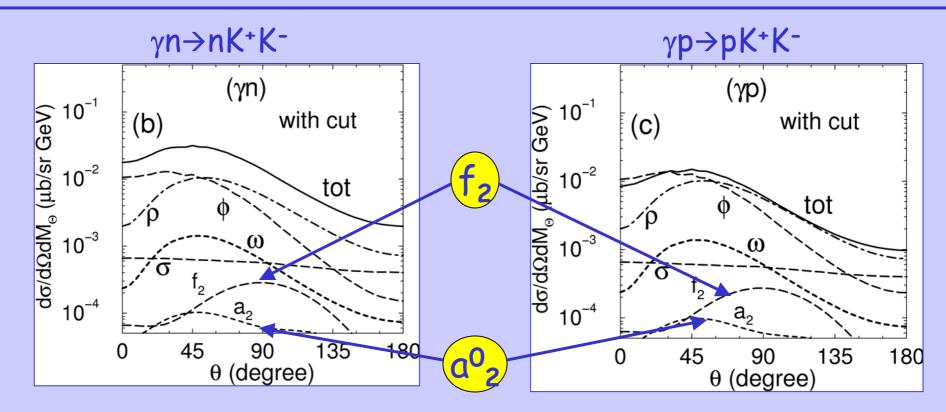
1.5

0 ∟ 1.4

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Tensor Meson Contribution

[A. Titov et al, nucl-th/0410098]



• The contributions from the tensor mesons, $f_2(1275)$ and $a_2(1320)$, at $E_{\gamma} = 2 \text{ GeV}$ are found to be very small

Summary on Kinematic Reflections

[K. Hicks, V. Burkert, A. Kudryavtsev, IS, S. Stepanyan, hep-ph/0411265]

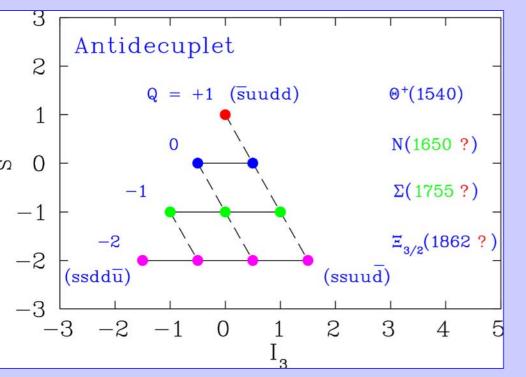
- There are considerable model assumptions that Dzierba *et al* have made
- The main exchange particle in their model is the pion (and its higher-mass partners on the Regge trajectory line)
 However, the π⁰ exchange contributions to production of f₂ and a⁰₂ are absent indeed, in either reggeized or non-reggeized versions of the model, thus diminishing the corresponding cross sections
- Calculations of kinematic reflections should be due to calculations that have had parameters fixed from on previous data (K⁺K⁻), rather than fit to the spectrum (nK⁺) where kinematic reflections are suspected

If Θ⁺ does not survive, `damned' questions revive:

- `Why are there no strongly bound exotic states..., like those of two quarks and two antiquarks or four quarks and one antiquark ?'
 [H. Lipkin, Phys Lett 45B, 267 (1973)]
- `...either these states will be found by experimentalists or our confined, quark-gluon theory of hadrons is as yet lacking in some fundamental, dynamical ingredient which will forbid the existence of these states or elevate them to much higher masses.'

[R. Jaffe and K. Johnson, Phys Lett 60B, 201 (1976)]

Tentative unitary Antidecuplet with Θ



 GMO: δm(σ) = (M_Ξ - M_Θ)/3 = 107 MeV at σ = 67 MeV [SAID] 180 MeV at σ = 45 MeV [Karlsruhe]

• Current δm corresponds to the GW SAID $\sigma\text{-term}$

• Mixing is able to shift GMO masses for N* and Σ^*

SAID: [M. Pavan *et al,* hep-ph/0111066] Karlsruhe: [G. Hoehler, Springer, 1983]

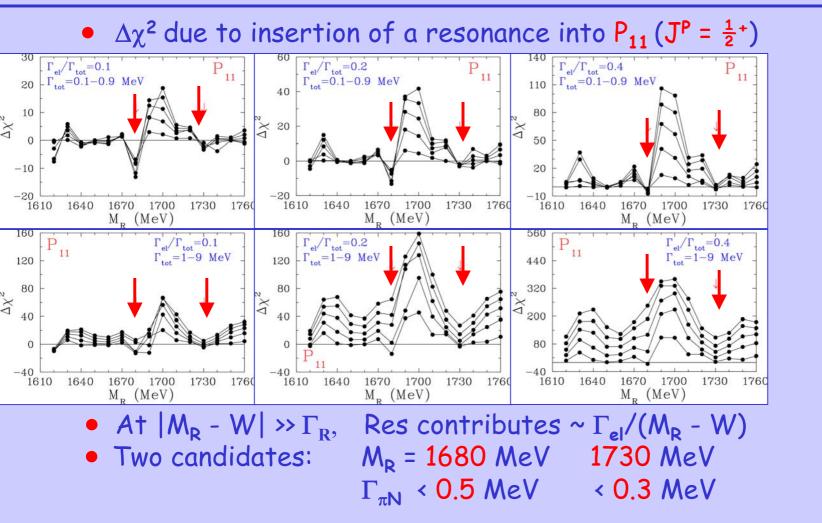
N(1710) – What was known

[PDG (S. Eidelman et al) Phys Lett B 592, 1 (2004)]

	Ref	Mass (MeV)	Width (MeV)
ChSA	DPP	1710 (input)	~40
PWA	KH	1723± 9	120± 15
	CMU	1700±50	90± 30
	KSU	1717±28	480±230
GW		no s	tate!

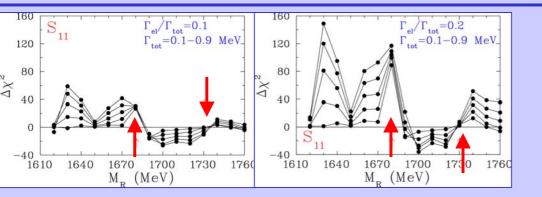
 It would be more natural for the same unitary multiplet (with ^{©+} and N^{*}) to have comparable widths

Modified $\pi N PWA$

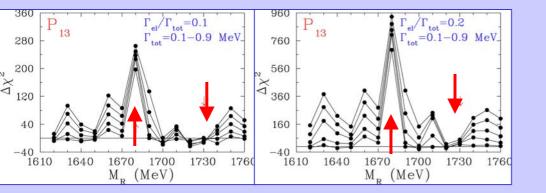


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Check other Partial Waves



• $\Delta \chi^2$ due to insertion of a Res into S₁₁ (J^P = 1/2⁻)



• $\Delta \chi^2$ due to insertion of a Res into P₁₃ (J^P = 3/2⁺)

Conclusion from Modified $\pi N PWA$

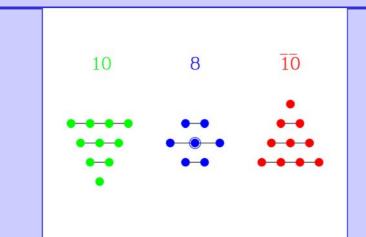
- 1680 MeV only one partial wave (P₁₁) reveals the effect: support to the resonance, $\Gamma_{\pi N} < 0.5$ MeV
- 1730 MeV P_{11} may also reveal a resonance with $\Gamma_{\pi N} < 0.3$ MeV but differently: resonance is still possible, if accompanied by different corrections
- Other partial waves, P_{13} and S_{11} (less probable), could show effect, if accompanied by different corrections

For example, thresholds: $N\omega(1720)$, $N\rho(1710)$?, $K\Sigma(1685)$

Theoretical Analysis

- Theoretical analysis is rather uncertain but nevertheless may be used for orientation
- Structure of hadron mixing due to violation of SU(3)_F
 - 10 \leftrightarrow 8 for Σ , Ξ (no partners for Λ , N, Δ)
 - 10 \leftrightarrow 8 for Σ , N (no partners for Λ , Θ , Ξ)
 - $10 \leftrightarrow 10$ for Σ (no partners for Δ, Θ, N, Ξ) Only higher orders in octet violation
 - Mixing shifts GMO masses of ⊕ partners may essentially influence decay widths
 - What are mixing with higher multiplets, such as 27 and/or 35?

Mixing



- Mixing is possible only for states with the same strangeness and isospin
- Mixing acts differently for different members of the 10

- $\Theta \rightarrow KN$ no mixing in the init state, 10-8 mixing is efficient in the fin state

- $N^* \rightarrow \pi \Delta$ no mixing in the fin state, 10-8 mixing is possible in the init state
- Mixing does not shift masses of Θ and $\Xi_{\rm 3/2},$ is able to shift GMO masses for
 - N*: 1650 MeV→1650-1690 MeV
 - Σ*: 1755 MeV→1760-1810 MeV
- [D. Diakonov, V. Petrov, Phys Rev D **69**, 094011 (2004)]

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Θ⁺ Flavor Partners

- If $\Gamma_{\Theta} \leq 1$ MeV, then expected structure for decays of the Θ -partners looks as follows:
- $\Gamma(N^* \rightarrow all) \sim 10 \text{ MeV } [\Gamma_{\pi N}/\Gamma_{tot} \leq 10 \%]$ Ratio of modes πN and ηN is sensitive to the mixing $\Gamma(N^* \rightarrow \pi \Delta) \sim 6 \text{ MeV } [forbidden for 10, open due to 10-8 mixing]$
- Σ^* is the most uncertain member of the 10, for both mass and width

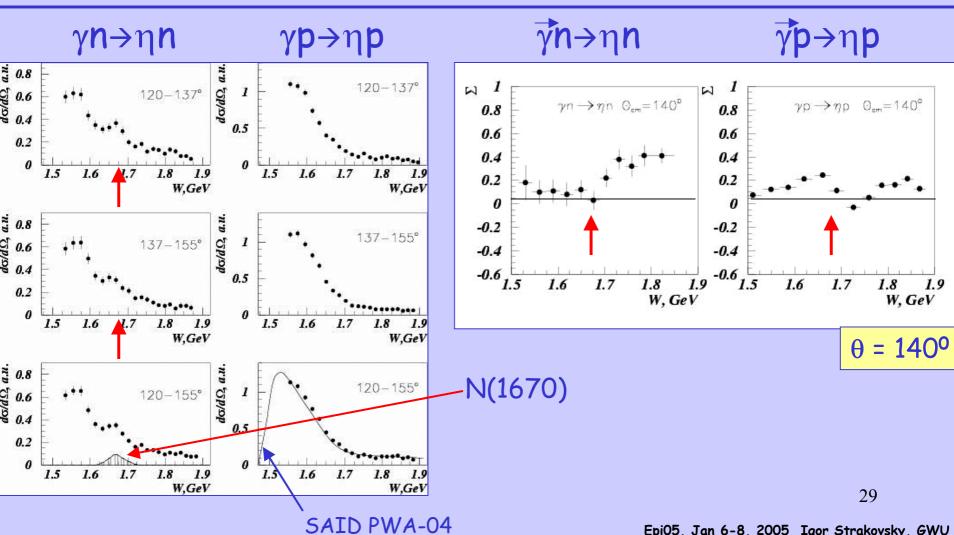
Estimates of partial widths are not very reliable, but at the level of `handwaving', $\Gamma(\Sigma^* \rightarrow all) \leq 30$ MeV

• For $\Xi_{3/2}$, estimates give general bound $\Gamma(\Xi_{3/2} \rightarrow all) \leq 5$ MeV Both Γ_{tot} and ratio of modes $\pi\Xi$ and $\overline{K\Sigma}$ are highly sensitive to the mixing

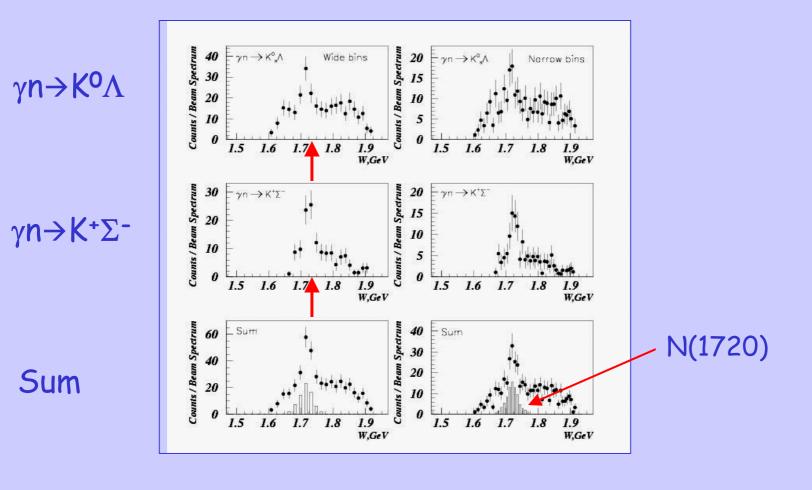
Experimental Evidences for N*

- GRAAL in $\gamma n \rightarrow \eta n$, K⁰A, and K⁺ Σ ⁻
- **STAR** in AuAu $\rightarrow \Lambda K_s$
- **COSY-TOF** in $pp \rightarrow \Lambda K^+ p$
- JLab Hall A in $H(e,e'\pi^+)X^0$

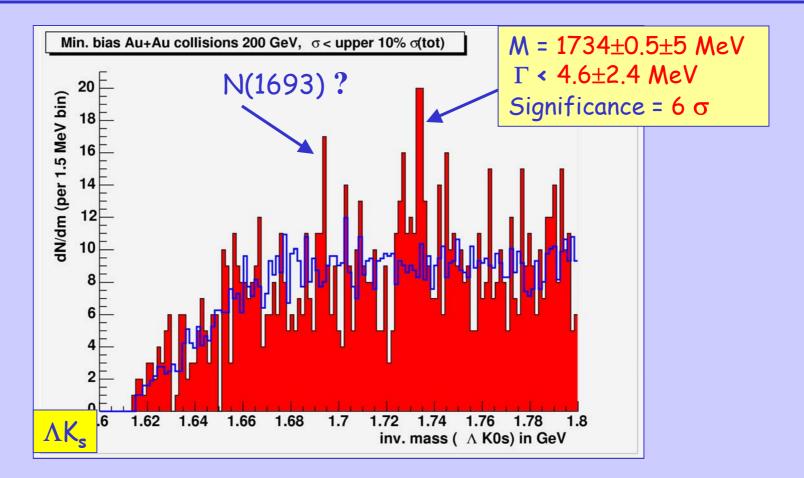
GRAAL [V. Kuznetsov, hep-ex/0409032, NSTAR 2004, March 2004] γn→ηn vs γp→ηp



GRAAL [V. Kuznetsov, Trento, Feb 2004] Very preliminary: $\gamma n \rightarrow K^0 \Lambda$, $K^+\Sigma^-$



STAR [S. Kabana, hep-ex/0406032, Jamaica, March 2004] $AuAu \rightarrow \Lambda K_s$



Summary

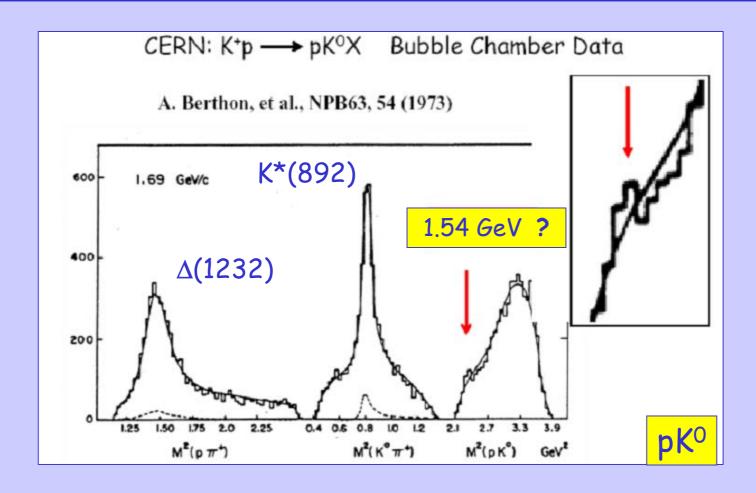
- Narrowness of Θ⁺ required reanalysis of all its flavor partners We did it for `N(1710)' using modified πN PWA
- If Θ^+ is indeed a narrow state with $\Gamma_{\Theta} \leq 1$ MeV, then other members of the flavor $\overline{10}$ are, most probably, narrow as well
 - Their properties are sensitive to the structure of mixing which can be rather complicated
- Studies of the 10 (and other non-qqq baryons) promise to be very interesting and exciting, though may appear not easy
- Direct precise measurements are necessary !!

Backup

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Unclaimed Θ^+ ?

[found by V. Burkert, Pentaquark 2003, Nov 2003]



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Was Progress delayed by Prejudice ? [PDG (M. Aguilar-Benitez *et al*) Phys Lett B **170**, 289 (1986)]

- "The evidence for strangeness +1 baryon resonances was reviewed in our 1976 edition [1], and more recently by Kelly [2] and by Oades [3]. Two new partial-wave analyses [4] have appeared since our 1984 edition. Both claim that the P₁₃ and perhaps other waves resonate.
- However, the results permit no definite conclusion the same story heard for 15 years. The standards of proof must simply be much more severe here than in a channel in which many resonances are already known to exist. The general prejudice against baryons not made of three quarks and the lack of any experimental activity in this area make it likely that it will be another 15 years before the issue is decided."

• References:

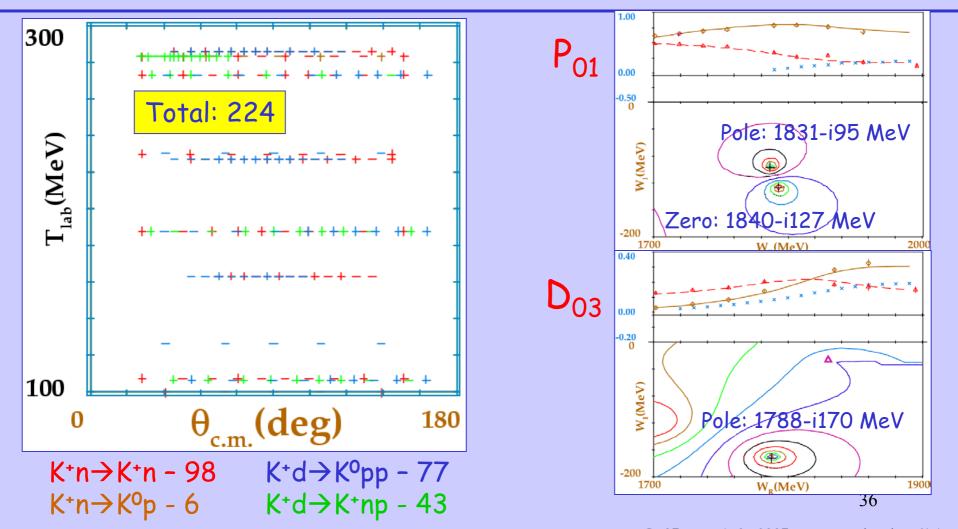
[1] Particle Data Group (T.G. Trippe *et al.*) Rev Mod Phys **48**, No 2, Part II (1976)

[2] R.L. Kelly, in Proceedings of the Meeting on Exotic Resonances (Hiroshima, 1978) edited by I. Endo et al.

[3] G.C. Oades, in Low and Intermediate Energy Kaon-Nucleon Physics (1981) edited by E. Ferrari and G. Violini

[4] K. Hashimoto, Phys Rev C 29, 1377 (1984); R.A. Arndt and L.D. Roper, Phys Rev D 31, 2230 (1985)

Standard PWA for K⁺n



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Conclusion from KN PWA

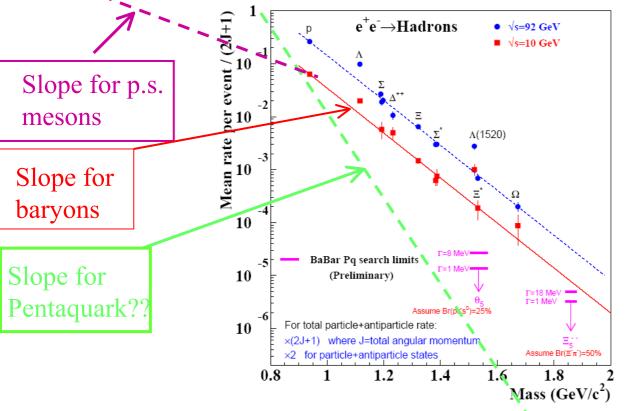
For I = 0:

- only one partial wave (P_{01}) admits the effect at 1540 - 1550 MeV: the resonance, $\Gamma < 1 - 2$ MeV

- other partial waves (S_{01} and P_{03}) may have the effect only by accompanied by other corrections



Hadron Production in e⁺e⁻ Analysis: V. Burkert, MENU 2004



Slope: **Pseudoscalar mesons:** ~10⁻²/GeV/c² (need to generate one qq pair)

Baryons: ~10⁻⁴ /GeV/c² (need to generate two pairs)

Pentaquarks: ~10⁻⁸ /GeV/c² (?) (need to generate 4 pairs)

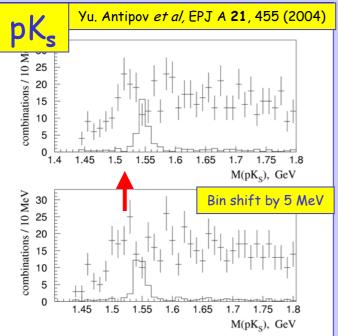
Pentaquark production in direct e⁺e⁻ collisions likely requires orders of magnitudes higher rates than available.

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• SPHINX vs HERMES [found by A. Dolgolenko]

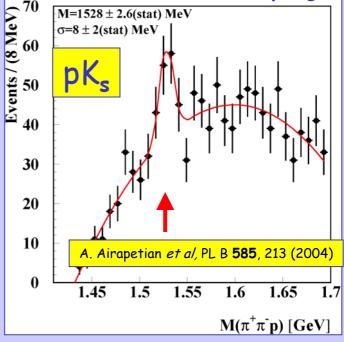
• SPHINX at IHEP: $pC(N) \rightarrow pK_sK_sN$



• Significance = 3.8σ

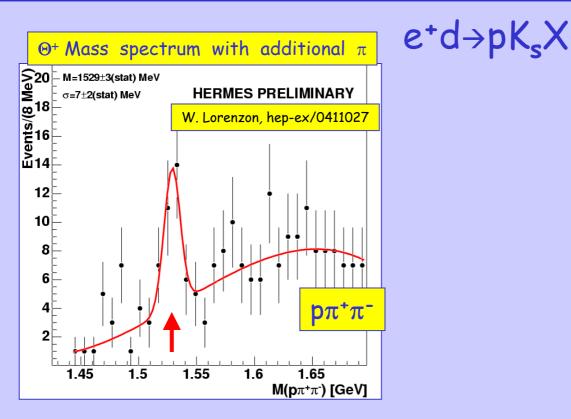
• HERMES at DESY:



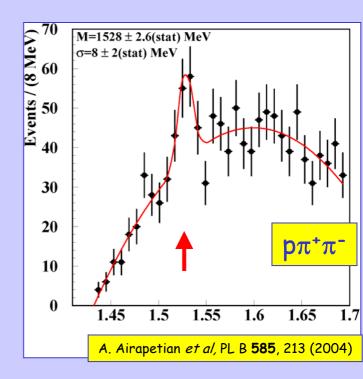


• Significance = $5.6\pm0.5 \sigma$

HERMES vs HERMES [W. Lorenzon, Pentaquark 2004, July 2004]

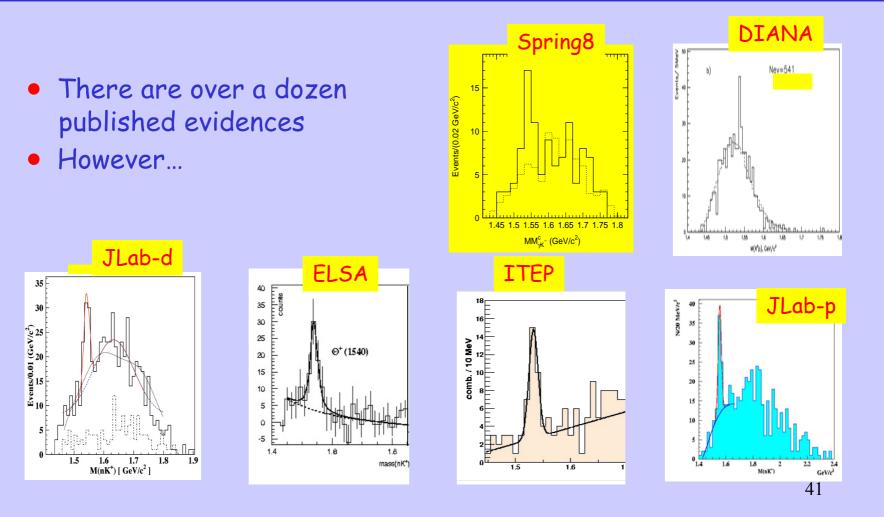


• Signal/Background= 2:1

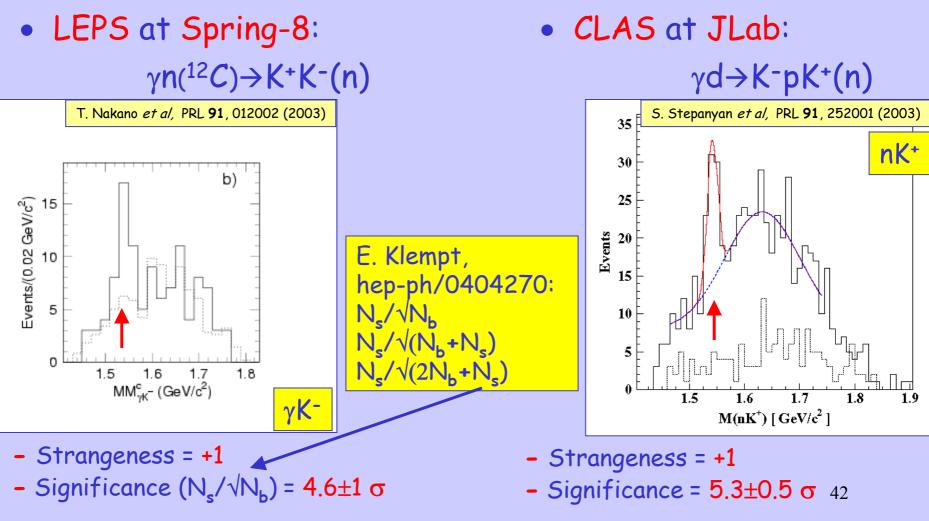


• Signal/Background= 1:3

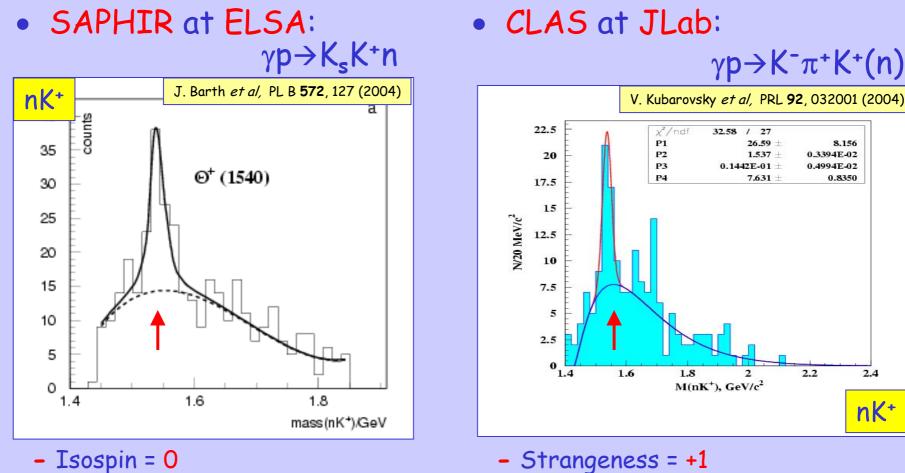
Was PDG right: 1986 + 15 = 2001±2 ?



Θ^+ Evidences with EM Probe



Θ⁺ Evidences with EM Probe



- Isospin = 0
- Significance = 4.8σ

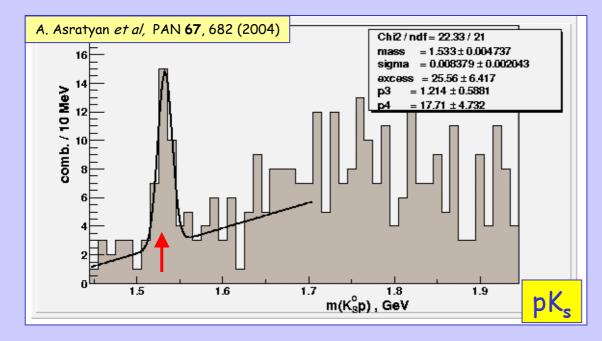
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- Significance = $7.8\pm1 \sigma$

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Θ^+ Evidences with Lepton Probe

• Reanalysis of Bubble Chamber Data from CERN and FNAL via ITEP: $v_{\mu}(\bar{v}_{\mu})A \rightarrow pK_sX$

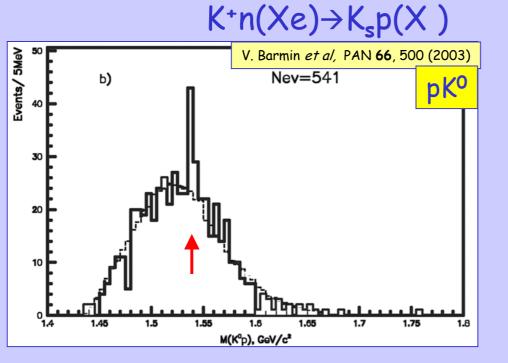


- Significance = 6.7σ

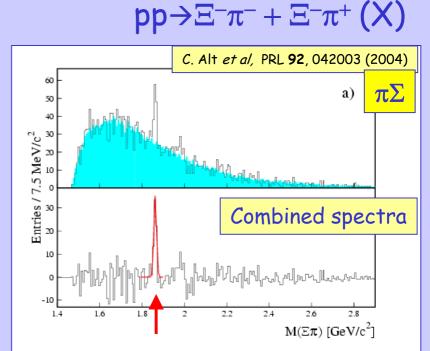
Θ^+ and Φ Evidences with Hadron Probes

• DIANA at ITEP:

NA49 at CERN:



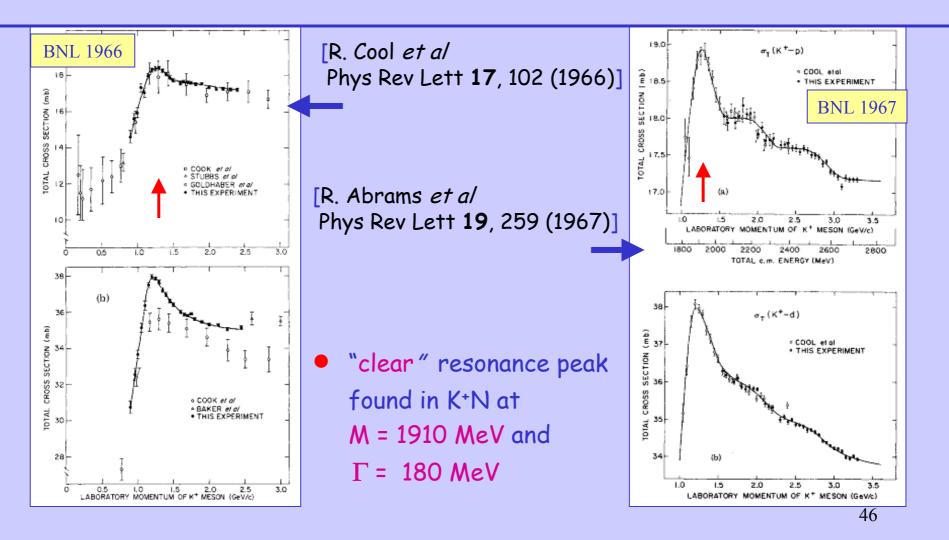
- Γ< 9 MeV
- Significance = 4.4σ



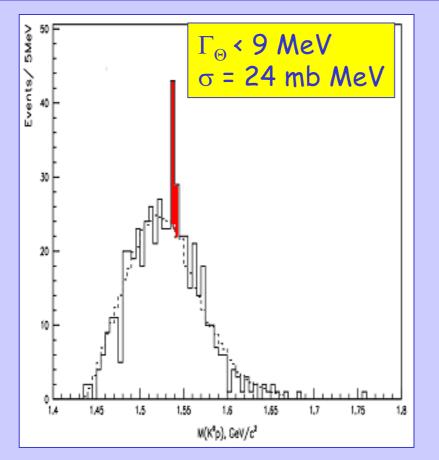
- Significance = 4σ

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First Search for Exotic Baryons in K⁺p and K⁺d



Analysis of the Xenon data



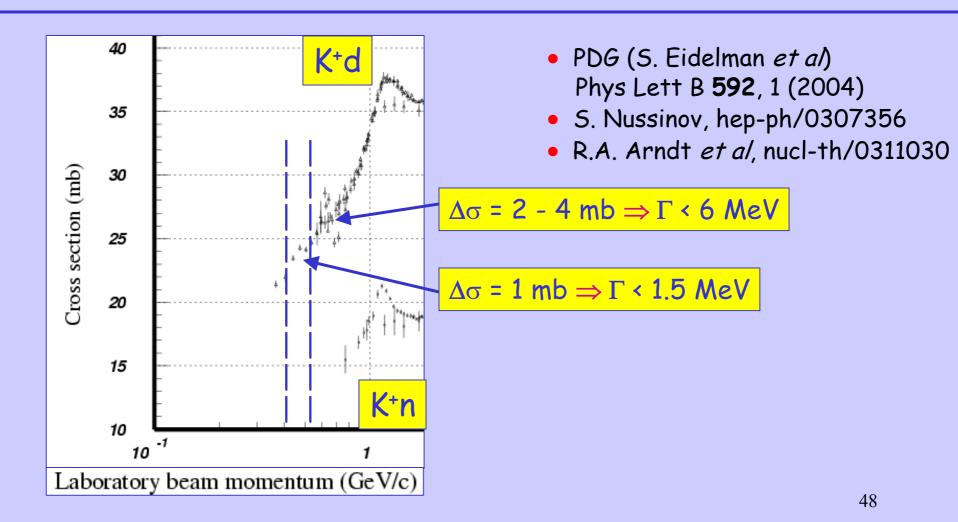
- R. Cahn and G. Trilling, PRD 69, 011501
- V. Barmin *et al*, PAN **66**, 1715 (2003)
- With additional assumptions and unknown systematics:

$$\sigma = B_i B_f \pi(\Gamma/2) \sigma_0 = 24 \text{ mb MeV}$$

 σ_0 (M=1540) = (2J+1)/(2s_N+1) (4 π /k²)= 68 mb

 $\Gamma = (2\sigma/\pi\sigma_0)(1/B_iB_f)= 0.9 \text{ MeV}$

Analysis of K⁺d σ^{tot}



BES [J. Bai *et al*, Phys Lett B 589, 7 (2004)]
 Analysis [Ya. Azimov, IS, Phys Rev C 70, 035210 (2004)]

• No double- or single- Θ production seen in decays of J/ψ and $\psi(2S) \rightarrow K_S pK^-n + ch.conj$.

• Double Θ (take branching into account: Br($\Theta \rightarrow K^+n$) = 1/2 and Br($\Theta \rightarrow K_sp$) = 1/4)

- Br($J/\psi \rightarrow \Theta \Theta$) < 0.44 × 10⁻⁴

Compare: $J/\psi \rightarrow \Sigma(1530)\Sigma(1530)$ kinematically similar, but not studied $Br(J/\psi \rightarrow \Lambda \overline{\Lambda}) \quad < (13.0\pm1.2) \times 10^{-4}$

 $\Theta\overline{\Theta}$ vs. $\Lambda\overline{\Lambda}$ - 2 more quark pairs, much smaller phase space ($M_{J/\psi}$ = 3097 MeV, $M_{th}(\Theta\overline{\Theta})$ = 3080 MeV)

- $Br(\psi(2S) \rightarrow \Theta \Theta) < 0.34 \times 10^{-4}$ Compare: $Br(\psi(2S) \rightarrow \Lambda \Lambda) = (1.81 \pm 0.34) \times 10^{-4}$

• Single (again, recall branchings)

- The most stringent boundaries $Br(J/\psi \rightarrow K^{0}p\overline{\Theta}) < 0.44 \times 10^{-4}$ $Br(\psi(2S) \rightarrow K^{0}p\overline{\Theta}) < 0.24 \times 10^{-4}$ *Compare:* $Br(J/\psi \rightarrow K^{-}p\overline{\Lambda}) = (8.9\pm1.6) \times 10^{-4}$ $Br(\psi(2S) \rightarrow \pi^{0}p\overline{p}) = (1.4\pm0.5) \times 10^{-4}$

• Summary on Θ^+ Nonobservation at BES

- Data need some (rather soft) dynamical suppression, say
 1/5 in the probability
- Meanwhile, because of necessity to produce directly two more qq pairs (in exotic decays as compared with decays to canonical baryon-antibaryon pairs), some dynamical suppression should naturally arise.
 One or two order suppression might be quite natural
- Thus, the recent result of BES is only a starting point for investigating exotics in e⁺e⁻-annihilation

Θ^+ Flavor Partner, N*(J^P = $\frac{1}{2}^+$)

- If $\Gamma_{\Theta} \leq 1$ MeV, then expected structure for decays of the Θ -partner N* looks as follows:
 - $\Gamma(N^* \rightarrow \pi \Delta) \sim 6$ MeV [forbidden for $\overline{10}$, open due to $\overline{10}$ -8 mixing]
 - Γ(N*→ηN) ~ 0.5 2 MeV
 - Γ(N*→KΛ) ~ 0.5 1.5 MeV
 - $\Gamma(N^* \rightarrow \pi N) \sim 0.3 0.5$ MeV [non-trivial cancellation

due to mixing is required]

- $\Gamma(N^* \rightarrow \pi \pi N)$ [out of $\pi \Delta$] ?
- $\Gamma(N^* \rightarrow K\Sigma)$ is small ?
- $\Gamma(N^* \rightarrow all) \sim 10 \text{ MeV } [\Gamma_{\pi N}/\Gamma_{tot} \leq 10 \%]$ Ratio of modes πN and ηN are sensitive to the mixing

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Σ^* (again, recall $\Gamma_{\Theta} \leq 1 \text{ MeV}$)

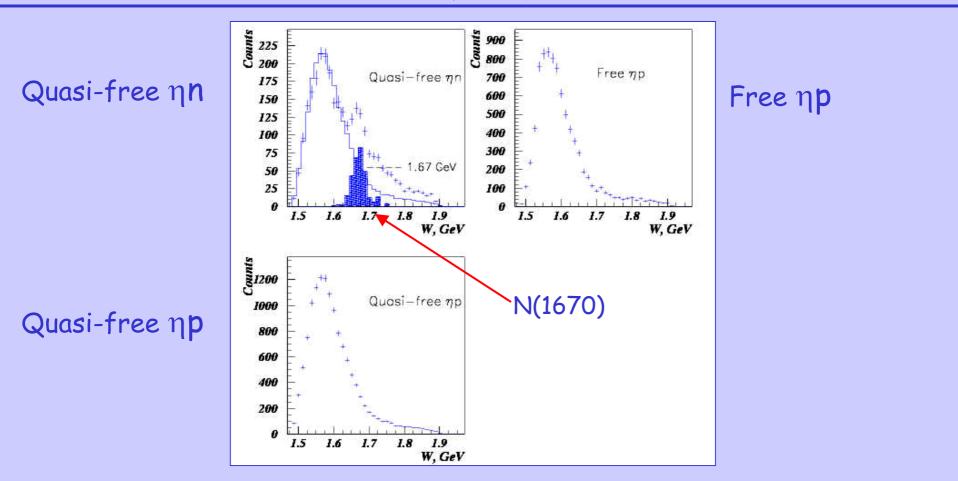
- The most uncertain member of the $\overline{10}$, for both mass and width
- Most decay modes may be essentially influenced by mixing in either initial and/or final states
- Estimates of partial widths are not very reliable, but at the level of `handwaving'
 Γ(Σ*→all) ≤ 30 MeV

$\Xi_{3/2}$ (again, recall $\Gamma_{\Theta} \leq 1 \text{ MeV}$)

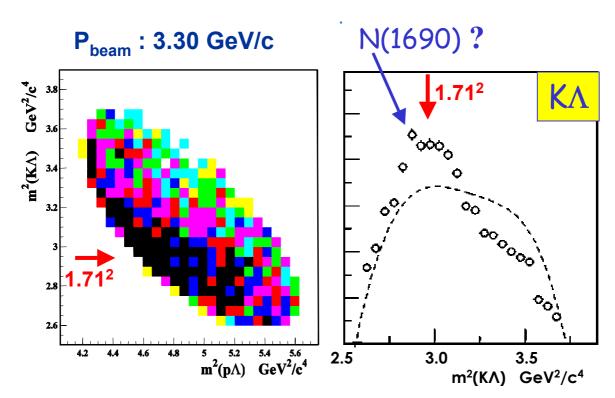
- Kinematically possible decays: Ξ_{3/2}→πΞ(1530) forbidden by SU(3)_F (10→8+10) could be allowed by (small !) mixing 10-8 for Ξ(1530), and/or mixing of Ξ_{3/2} with 27, 35, ... Γ(Ξ_{3/2}→πΞ) practically independent of mixing Γ(Ξ_{3/2}→KΣ) essentially depends on the final state mixing
- Estimates give general bound $\Gamma(\Xi_{3/2} \rightarrow all) \le 5 \text{ MeV}$
- Both Γ_{tot} and ratio of modes $\pi \Xi$ and $\overline{K}\Sigma$ are highly sensitive to the mixing

GRAAL [V. Kuznetsov, hep-ex/0409032, NSTAR 2004, March 2004]

γn→ηn



COSY-TOF [W. Eyrich, Pentaquark 2004, July 2004] Very preliminary: $pp \rightarrow \Lambda K^+ p$

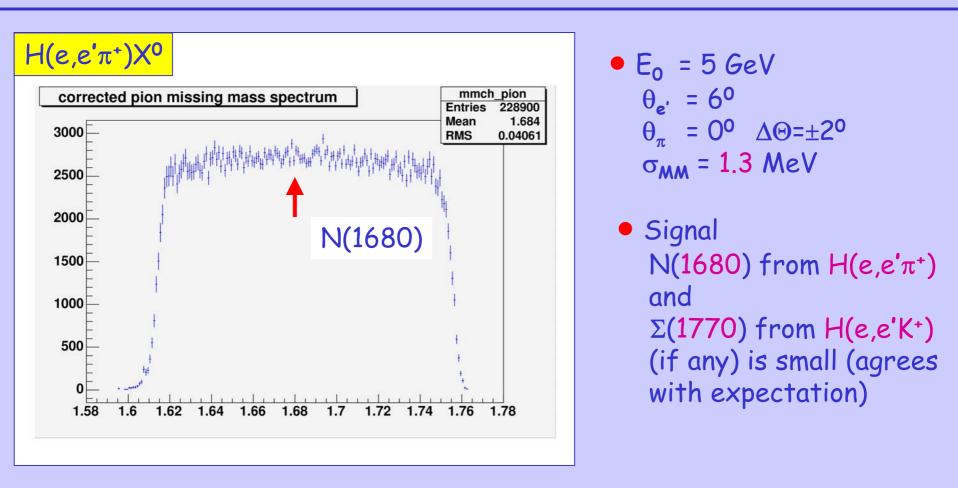


N*(1710) contributes strongly

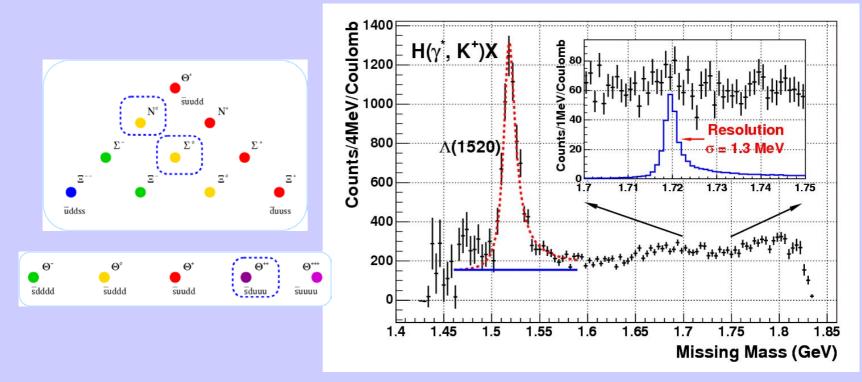
Influence of $p\Lambda$ -FSI

In progress: Investigation of Dalitz plots -> width

JLab Hall A [B. Wojtsekhowski, E-04-012] Very preliminary, data taken in May of 2004



E04-012 Search for Pentaquark Partners



Upper limits on production of narrow resonances

($\Gamma = 5 \sim 15 MeV$) at photon energy 3 GeV

•
$$\Sigma_5^o \qquad \sigma / \sigma(\Lambda_{1520}) < 1.7\%$$

• Θ^{++} $\sigma/\sigma(\Lambda_{1520}) < 0.8\%$

Lattice

- The lattice gauge theory is the only QCD based approach which pretends to do hadron spectroscopy computations directly from the first principles
- However as far as we know, in the current lattice literature there exist three various statements:

The ⊕⁺ has J^P=1/2⁺ (1 group)
 The ⊕⁺ has J^P=1/2⁻ (5 groups)
 The ⊕⁺ does not exist at all (2 groups)

• Therefore, it is worth of referencing

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